

Analysing Survival Endpoints in Randomized Clinical Trials using Generalized Pairwise Comparisons

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Hospices Civils de Lyon

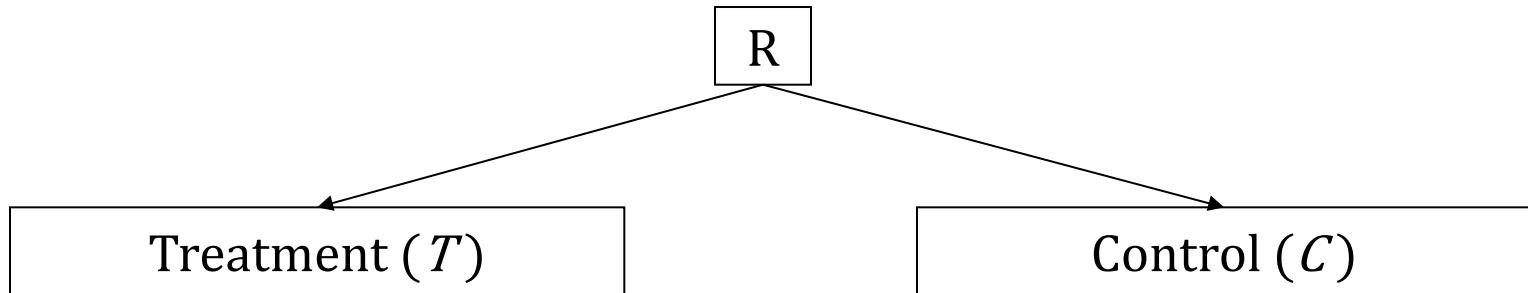
Outline

- The standard procedure of generalized pairwise comparisons
- An extension for right-censored data
- A patient-oriented measure of treatment benefit
- Benefit-risk balance
 - NCIC PA.3 trial => erlotinib in pancreatic cancer

Outline

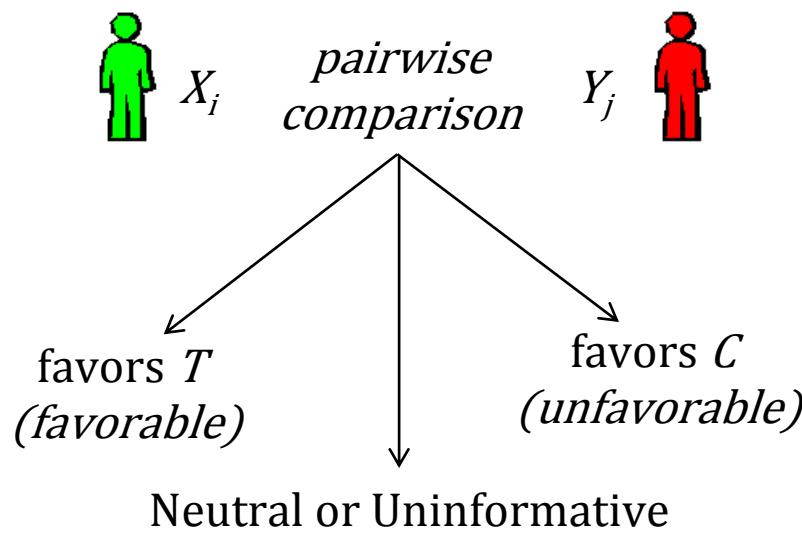
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Methods – Pairwise comparisons



Let x_i be the outcome of
 i^{th} subject in T ($i = 1, \dots, n$)

Let y_j be the outcome of
 j^{th} subject in C ($j = 1, \dots, m$)



Methods – Definition of thresholds

Coutinuous outcome

Pair	Rating
$x_i - y_j > \tau$	Favorable
$x_i - y_j < (-\tau)$	Unfavorable
$ x_i - y_j \leq \tau$	Neutral
x_i or y_j missing	Uninformative

Methods – Definition of priority

First priority outcome	Second priority outcome	Pair rating
Favorable	NA	Favorable
Unfavorable	NA	Unfavorable
Neutral/Uninf	Favorable	Favorable
Neutral/Uninf	Unfavorable	Unfavorable
Neutral/Uninf	Neutral/Uninf	Neutral/Uninf

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Neutral/Uninf	Unfavorable	Unfavorable
Neutral/Uninf	Neutral/Uninf	Neutral/Uninf

Methods – Standard procedure for pairwise scoring

$$U_{ij} = \begin{cases} +1 & \text{when the pair } (X_i, Y_j) \text{ is favorable} \\ -1 & \text{when the pair } (X_i, Y_j) \text{ is unfavorable} \\ 0 & \text{otherwise} \end{cases}$$

$$\Delta = U = \frac{1}{m \cdot n} \sum_{i=1}^n \sum_{j=1}^m U_{ij}$$

Δ is named «net chance of a better outcome»

Some notations

- x_i^0 and y_j^0 : time-to-event
- x_i and y_j : time-to-observation
- Event indicator :

$$\delta_i = \begin{cases} 1 & \text{if } x_i = x_i^0 \\ 0 & \text{if } x_i < x_i^0 \end{cases} \quad \text{in group T}$$
$$\varepsilon_j = \begin{cases} 1 & \text{if } y_j = y_j^0 \\ 0 & \text{if } y_j < y_j^0 \end{cases} \quad \text{in group C}$$

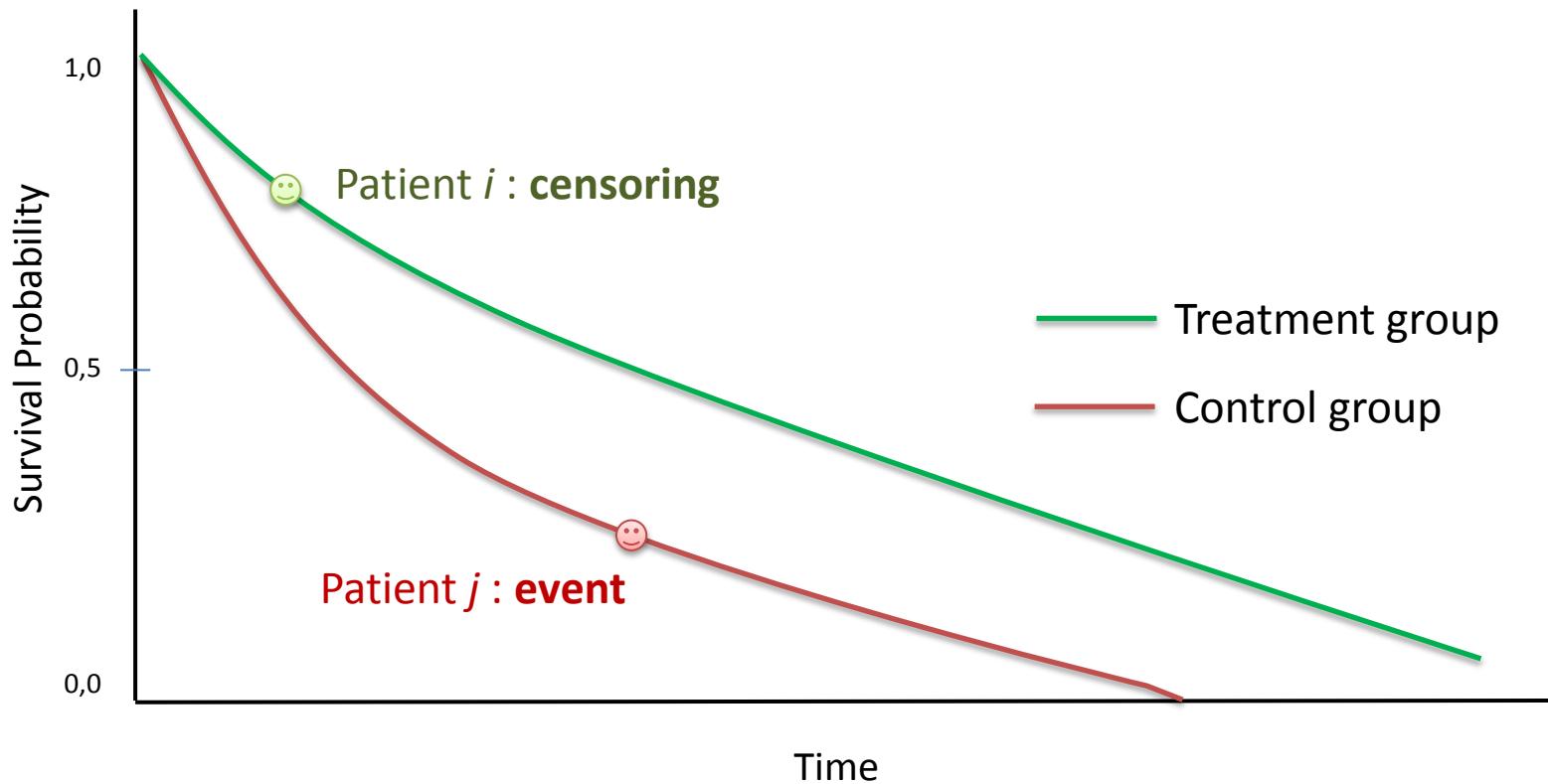
- Survival function:

$$S_{Ttt}(t) = \mathbb{P} [x_i^0 \geq t] \text{ and } S_{Ctrl}(t) = \mathbb{P} [y_j^0 \geq t]$$

The standard procedure to include time-to-event' outcome

$(\delta_i, \varepsilon_j)$	$x_i - y_j \geq \tau$	$x_i - y_j \leq -\tau$	$ x_i - y_j < \tau$
(1, 1)	Favorable	Unfavorable	Neutral
(0, 1)	Favorable	Uninformative	Uninformative
(1, 0)	Uninformative	Unfavorable	Uninformative
(0, 0)	Uninformative	Uninformative	Uninformative

The standard procedure to include time-to-event outcome

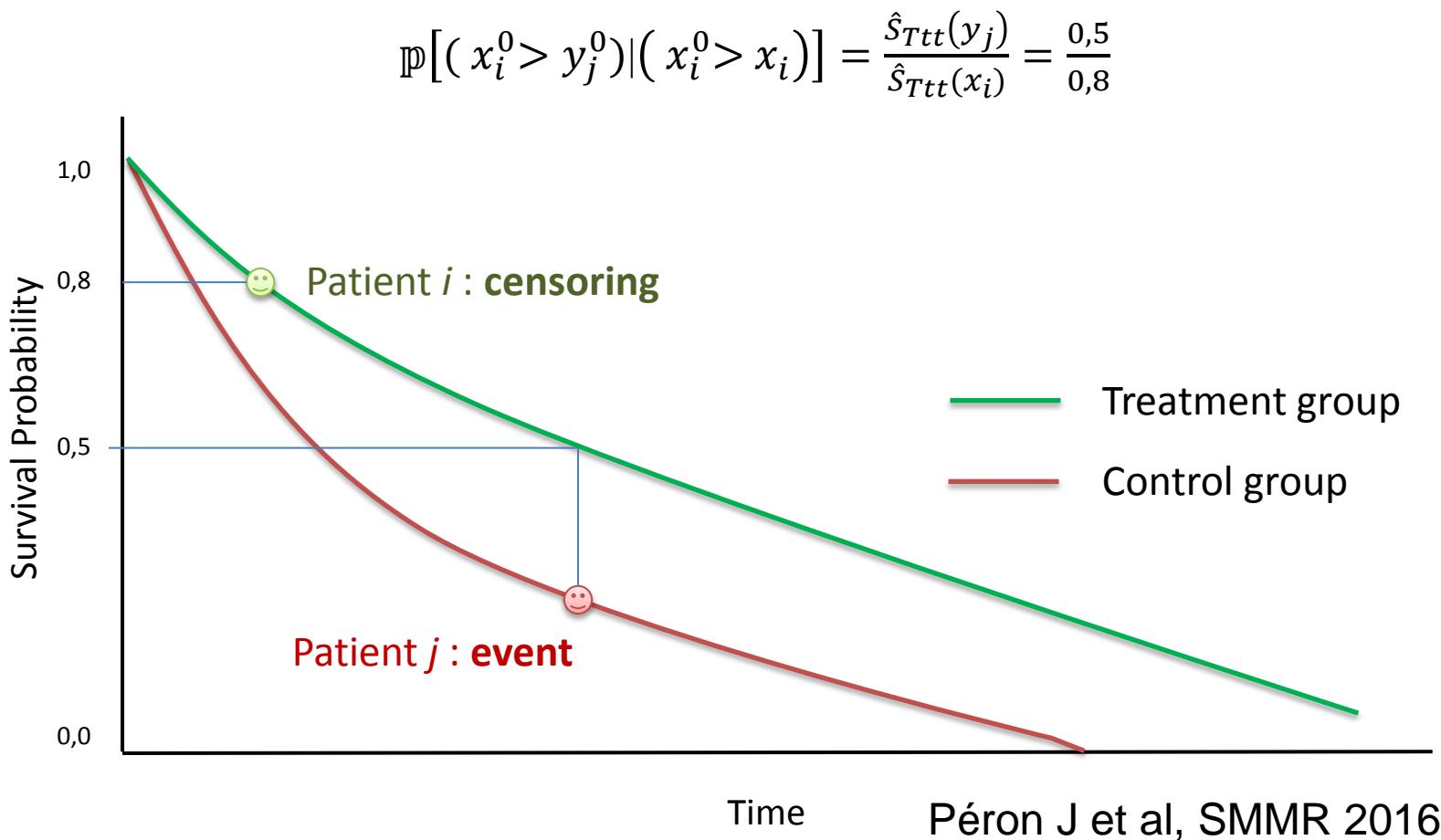


Outline

- The standard procedure of generalized pairwise comparisons
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The extended procedure taking into account 'non-informative' pairs

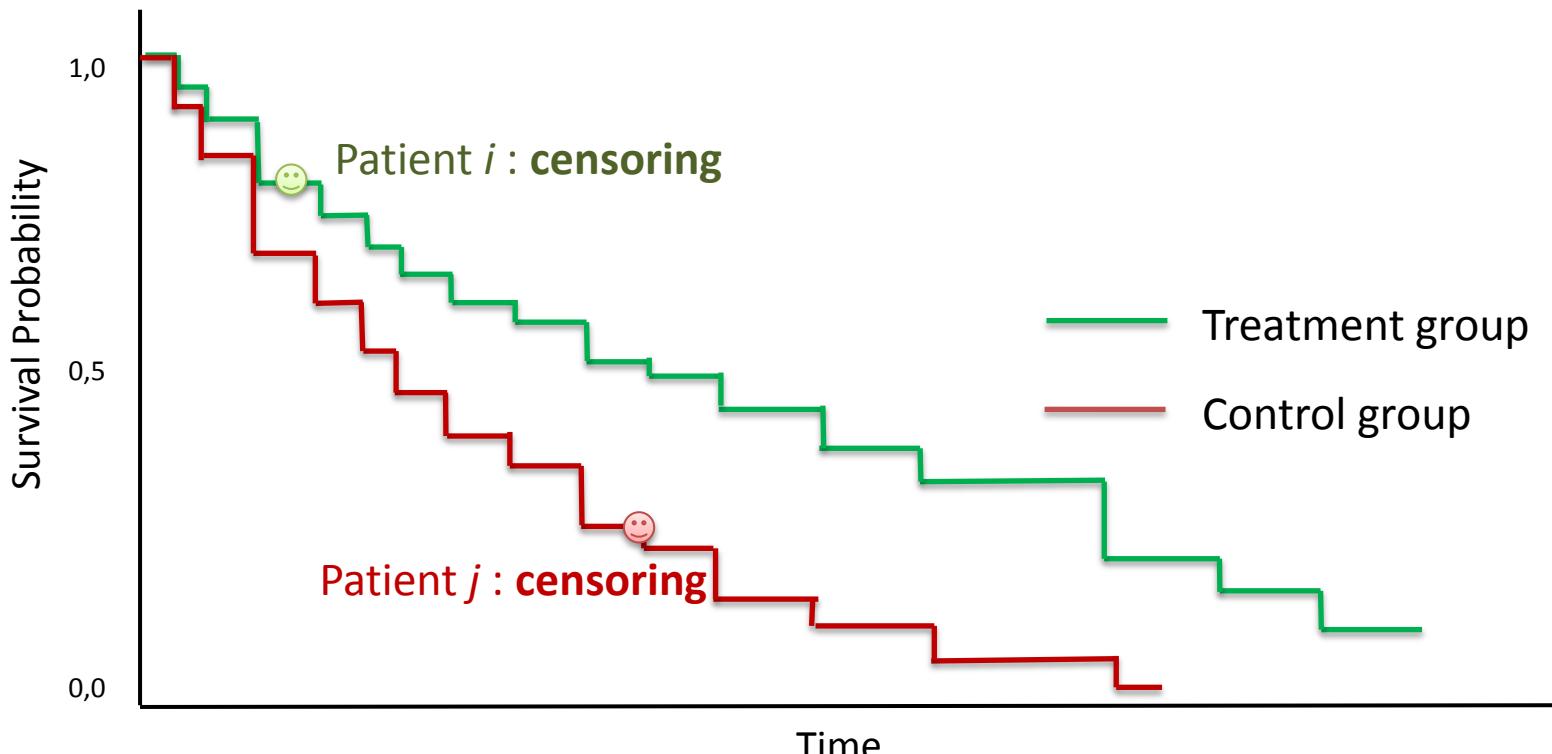
Based on the Kaplan-Meier estimate of the survival function



The extended procedure taking into account 'non-informative' pairs

When the estimation of the survival function is discontinue :

$$\mathbb{P}[(x_i^0 > y_j^0) | (x_i^0 > x_i), (y_j^0 > y_j)] = - \sum_{t > y_j}^{\infty} \frac{\hat{S}_{Ttt}(t)}{\hat{S}_{Ttt}(x_i) \hat{S}_{Ctrl}(y_j)} \cdot (\hat{S}_{Ctrl}(t^+) - \hat{S}_{Ctrl}(t^-))$$



The extended procedure taking into account ‘non-informative’ pairs

For pairs that can not be decidedly classified because of censoring, we compute:

$$\mathbb{P}(x_i^0 > y_j^0 + \tau), \text{ et } \mathbb{P}(y_j^0 > x_i^0 + \tau), \text{ et } \mathbb{P}(|x_i^0 - y_j^0| < \tau)$$

The pairwise score is:

$$s_{ij} = \mathbb{P}(x_i^0 > y_j^0 + \tau) - \mathbb{P}(y_j^0 > x_i^0 + \tau)$$

The net chance of a better outcome is then:

$$\hat{\Delta} = \frac{1}{m \cdot n} \sum_{i=1}^n \sum_{j=1}^m s_{ij}$$

The pairwise weight the analysis of an outcome of lower priority is:

$$\omega_{ij} = \mathbb{P}(|x_i^0 - y_j^0| < \tau)$$

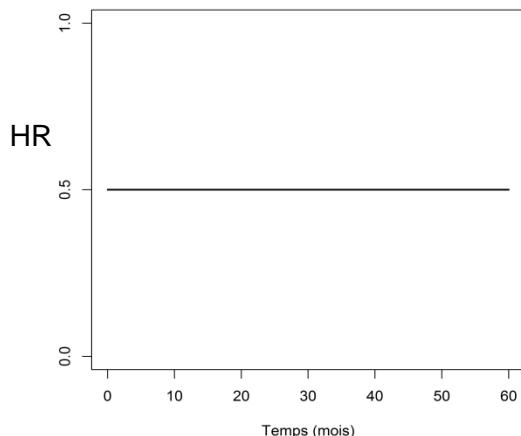
Simulation study - Design

- **Objective:** To compare the standard and the extended procedures of generalized pairwise comparison
- Simulation of $M = 1000$ datasets of with $N = 200$ patients
 - One time-to-event outcome
 - Threshold $\tau = 0$ months

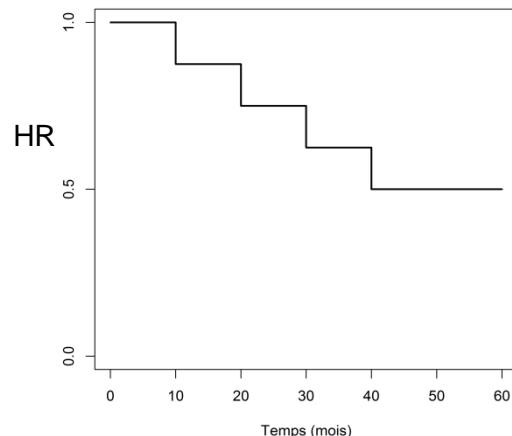
Simulation study - Design

- Survival time: exponential distributions

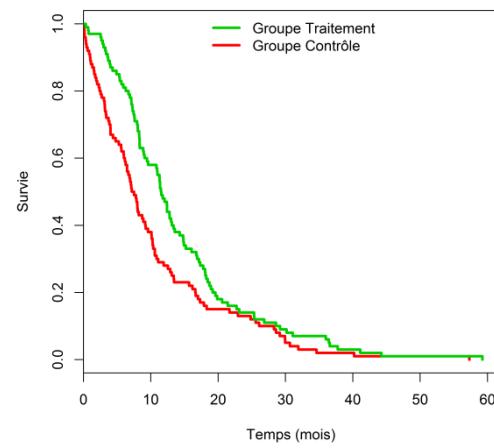
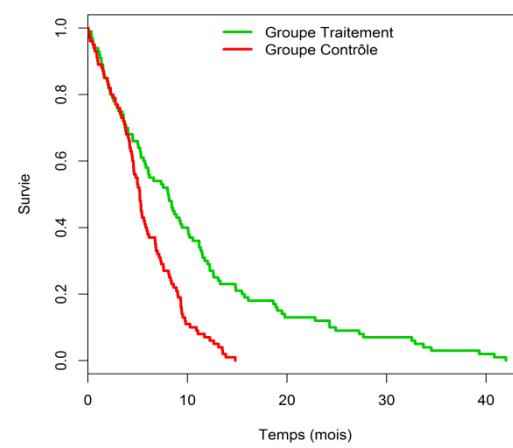
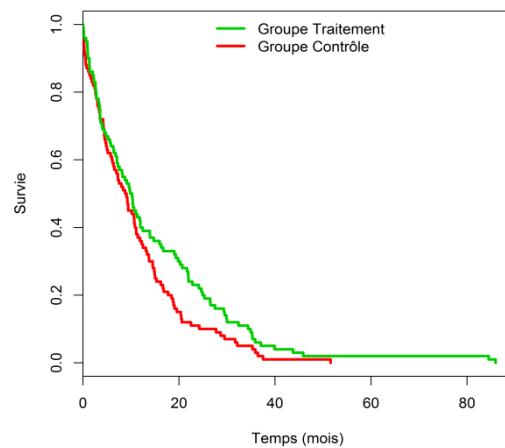
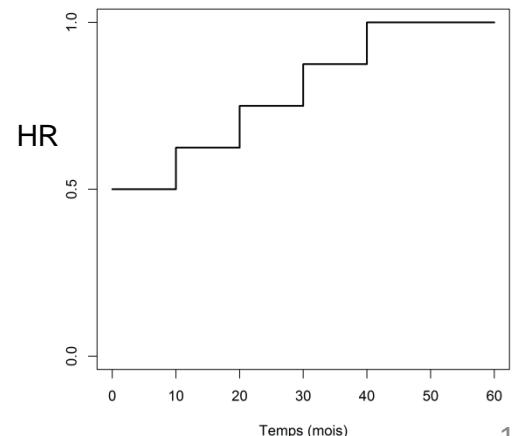
Scenario 1 : Proportional hazards



Scenario 2 : Late treatment effect



Scenario 3 : early treatment effect



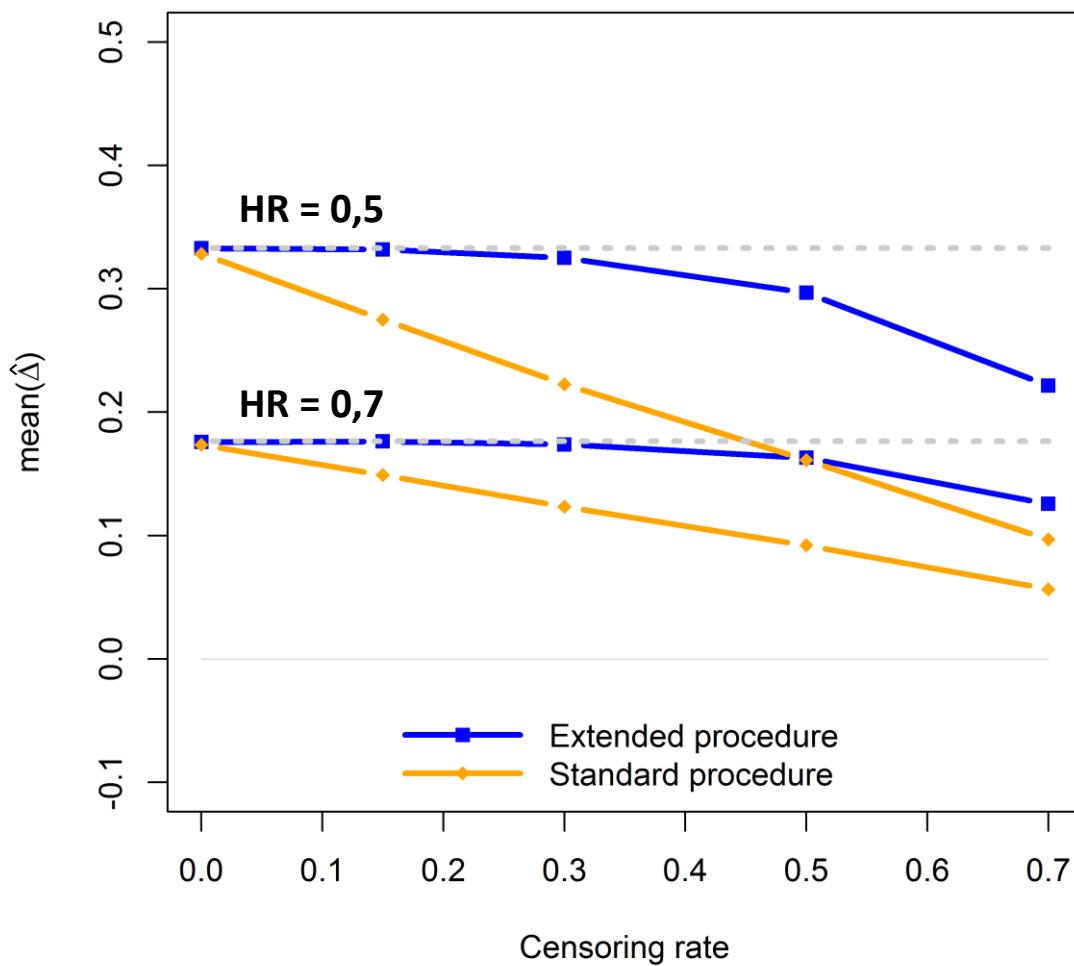
Simulation study - Design

- Several treatment effect sizes
 - Hazard ratio {0,5; 0,7; 1}
- Administrative censoring proportion
 - Uniform distribution
 - Between 0% and 70%

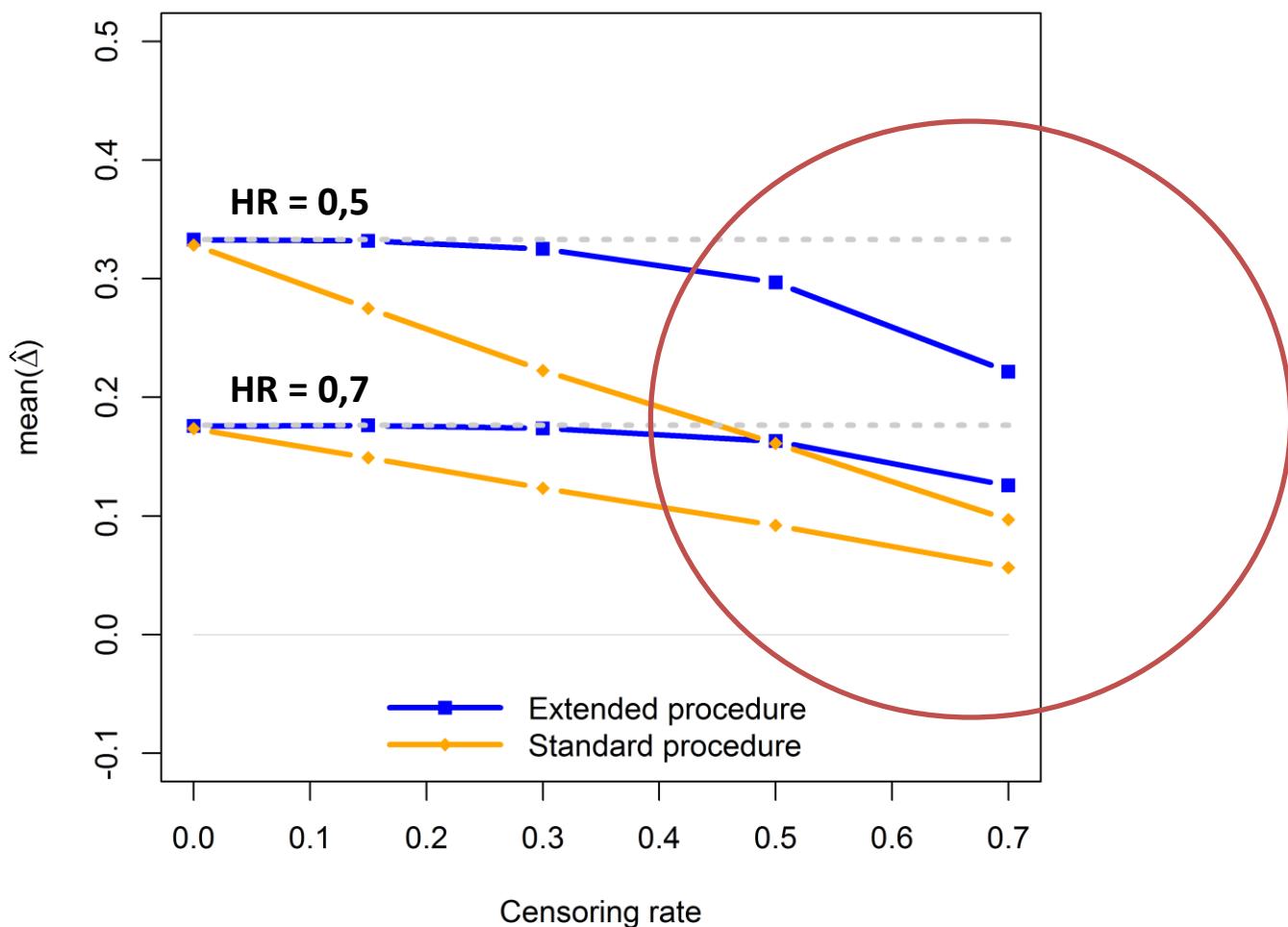
Simulation study - Design

- For each simulated dataset
 - Estimation of the net chance of a better outcome (standard and extended procedure)
 - Test of the null hypothesis (Permutation test, Log-Rank test)
- Endpoints
 - Bias
 - Power
 - Type 1 error

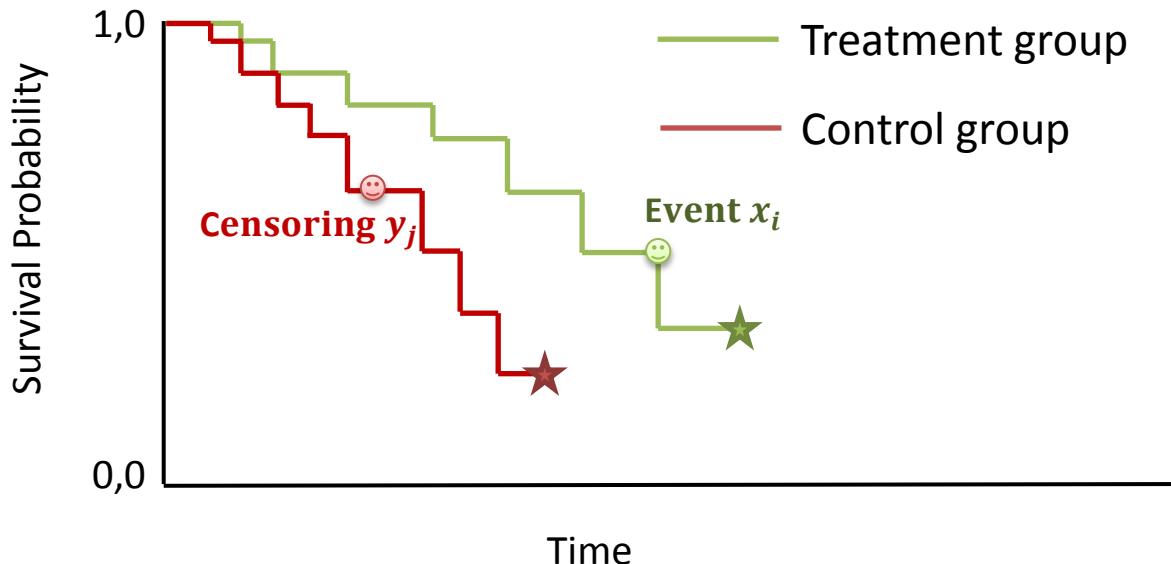
Scenario 1 – Proportionnal hazards



Scenario 1 – Proportionnal hazards



An explanation for this bias?



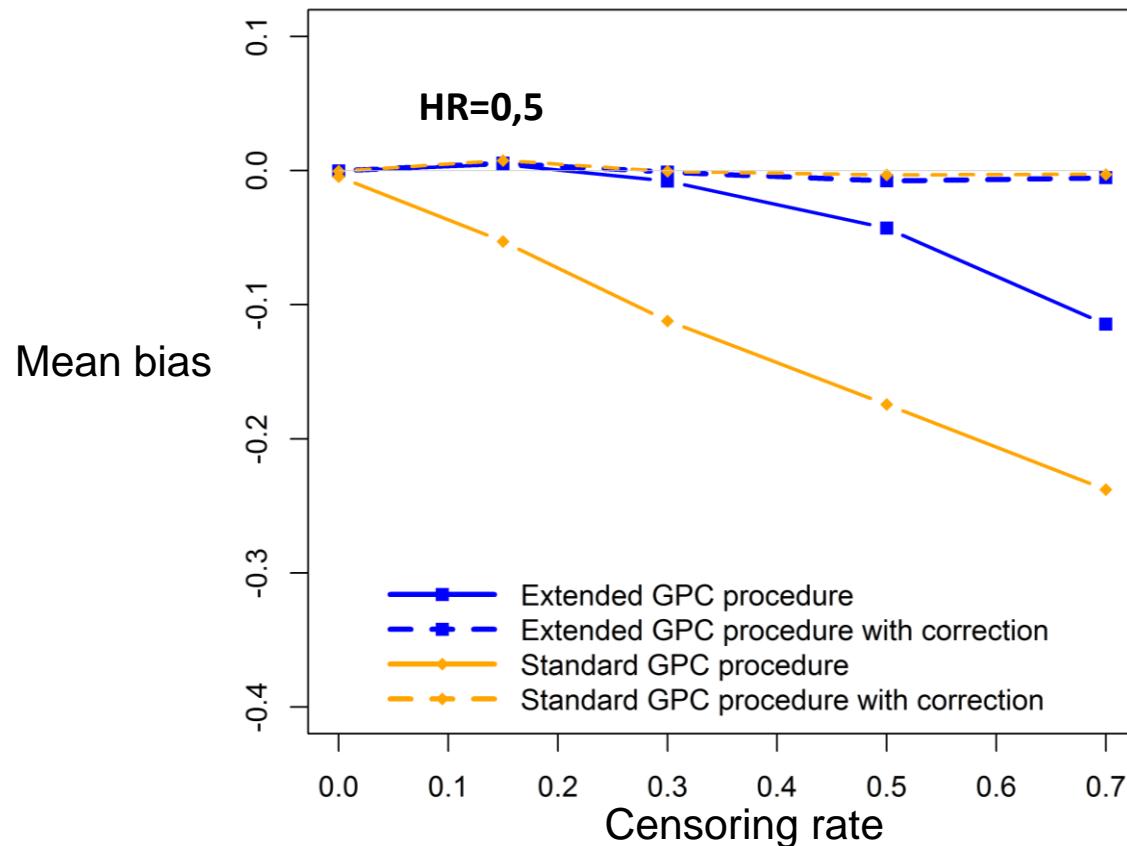
Standard procedure: **Uninformative** $\rightarrow p_{ij} = 0$

Extended procedure: $\begin{cases} \mathbb{P}[x_i^0 > y_j^0 + \tau] = 1 - \frac{\hat{s}_C(x_i - \tau)}{\hat{s}_C(y_j)} \\ \mathbb{P}[y_j^0 > x_i^0 + \tau] = \frac{\hat{s}_C(x_i + \tau)}{\hat{s}_C(y_j)} \end{cases}$ **Uninformative also** $\rightarrow p_{ij} = 0$

A correction for this bias

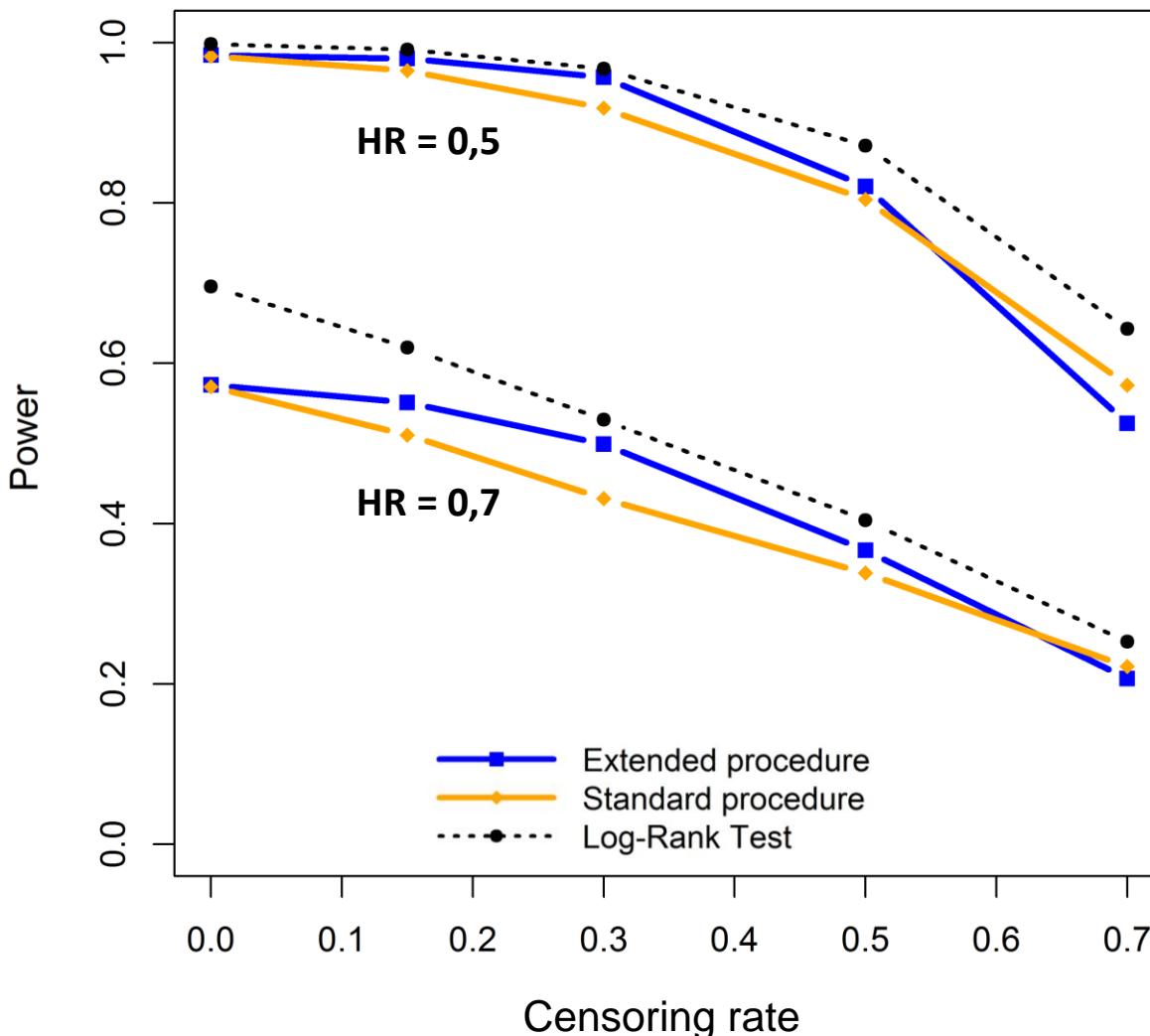
f_m : Proportion of informative pairs for the trial m ($m = 1, \dots, M$)

$\widehat{\Delta}corr_m = \frac{\widehat{\Delta}_m}{f_m}$: corrected net chance of a better outcome



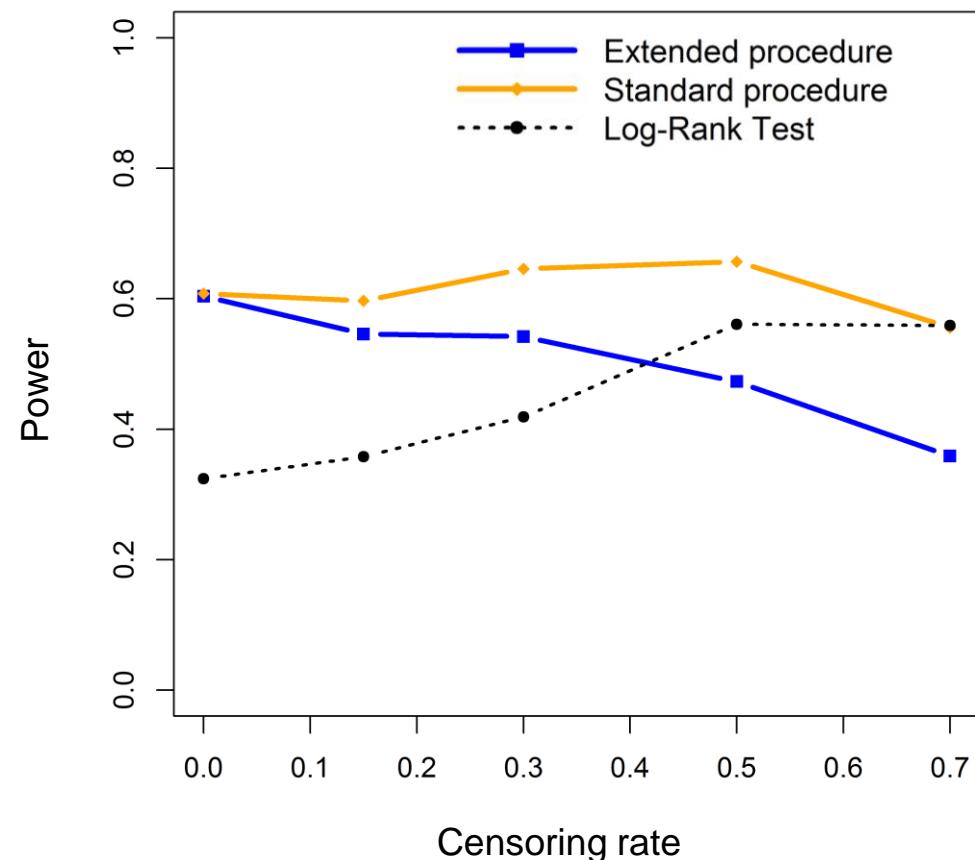
$$Bias = \mathbb{E}(\widehat{\Delta} - \Delta)$$

Scenario 1 – Proportional hazards

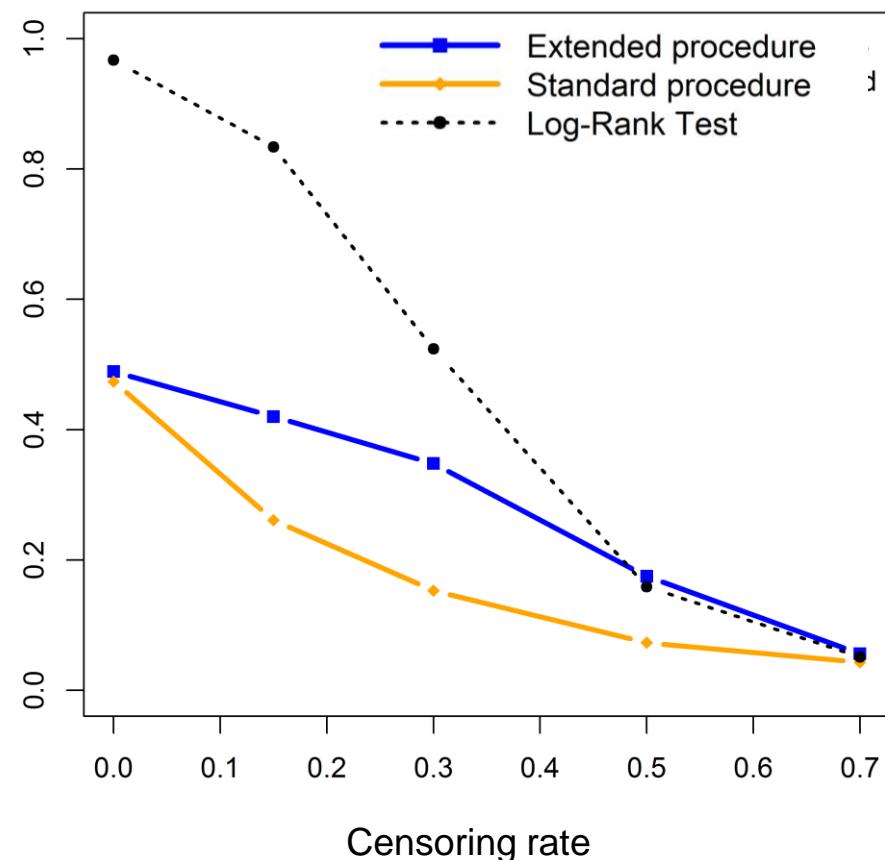


Scenario 2 et 3 – Non Proportional hazards

Early treatment effect



Late treatment effect



Type 1 error rate $\approx 5\%$

Conclusions of the simulation study

- Bias in the estimation of Δ
 - Less important
 - Correction available when only one endpoint
- Power of the permutation test extended procedure > standard procedure
 - Exponential distribution
 - Proportional hazards and administrative censoring $< 67\%$ (B Efron, Stanford Univ, 1967)
 - Late treatment effect

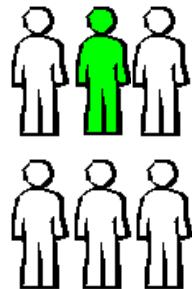
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The net chance of a better outcome

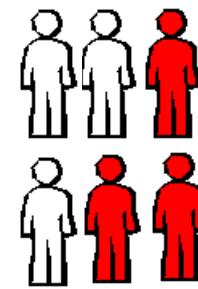
Probability for a random patient in the Treatment group to have a 'better outcome' than a random patient in the Control group ...

Treatment group



$$\Delta = \mathbb{P}(X > Y) - \mathbb{P}(Y > X)$$

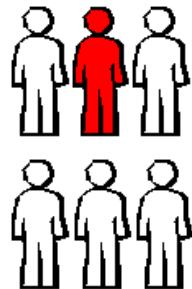
Control group



The net chance of a better outcome

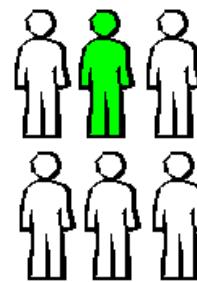
...minus the opposite probability.

Treatment group



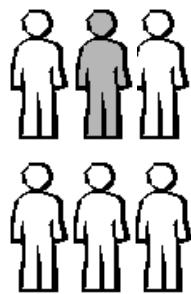
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Control group



The net chance of a better outcome

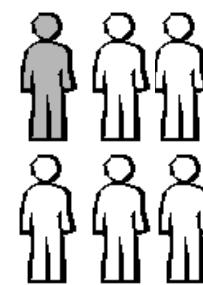
Treatment group



$$\mathbb{P}(Y = X)$$

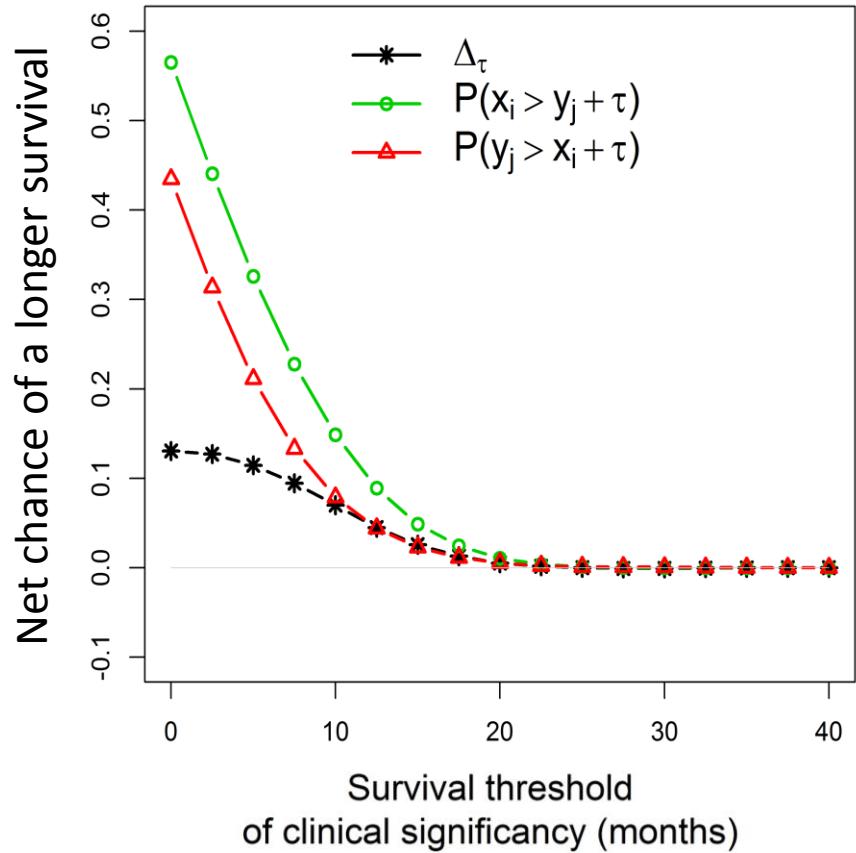
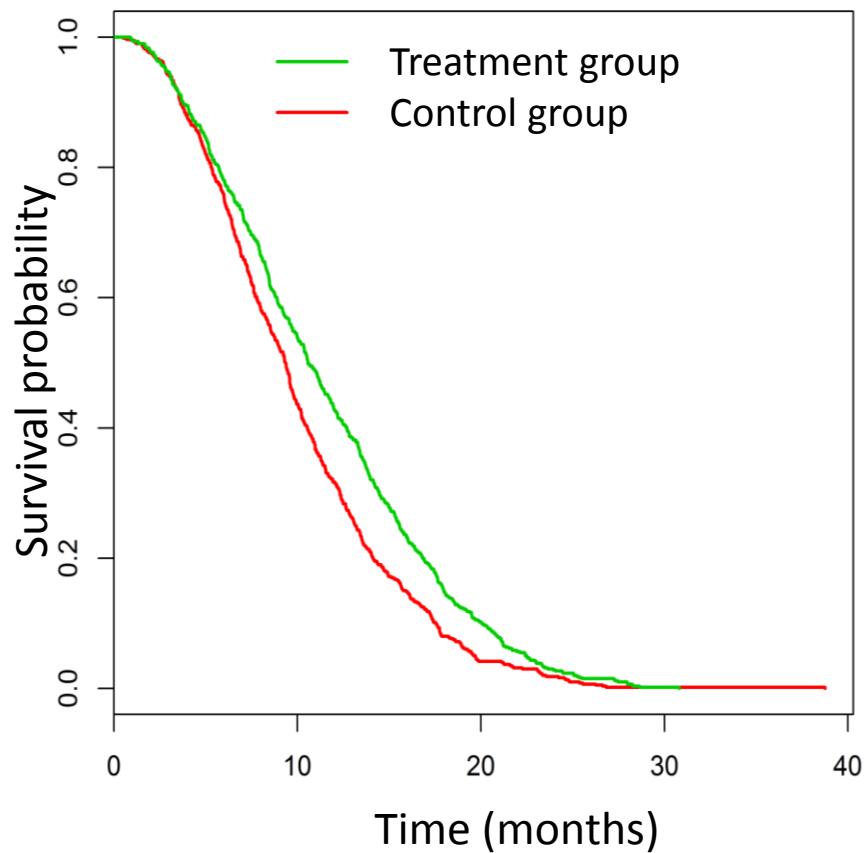
$$\Delta = \mathbb{P}(X > Y) - \mathbb{P}(Y > X)$$

Control group



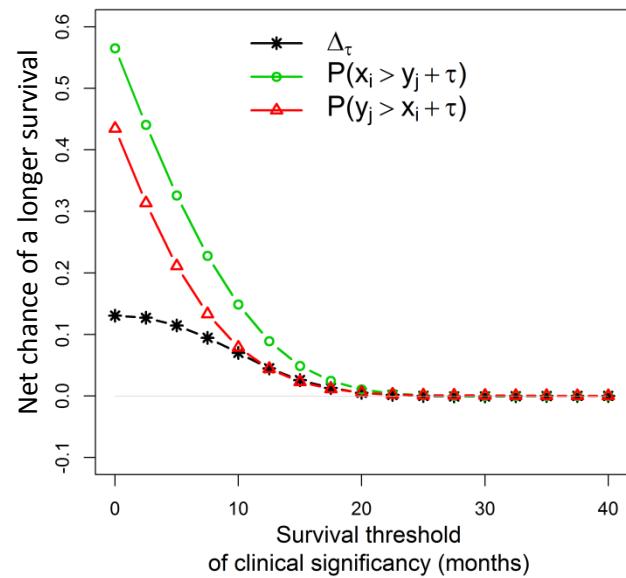
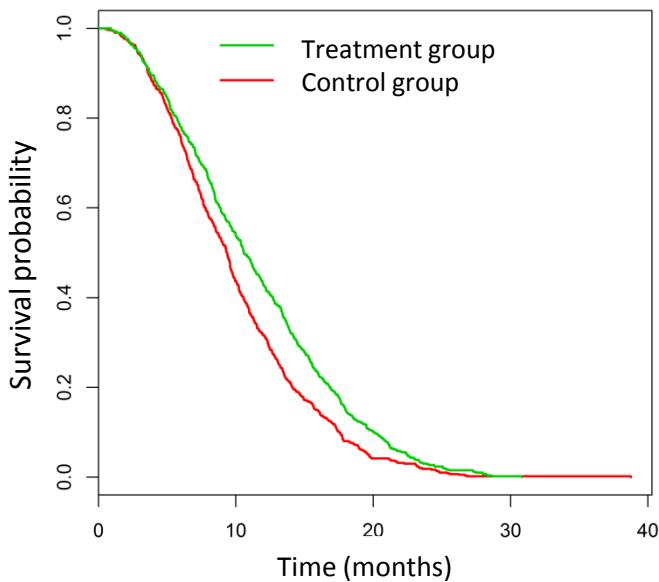
The net chance of a longer survival

Proportional hazards

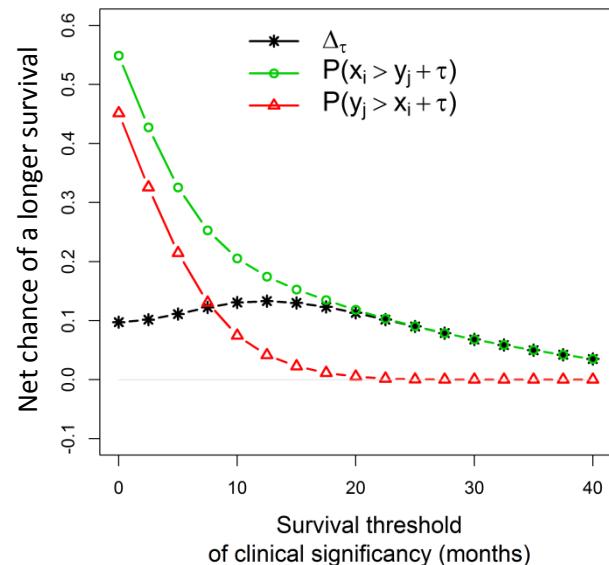
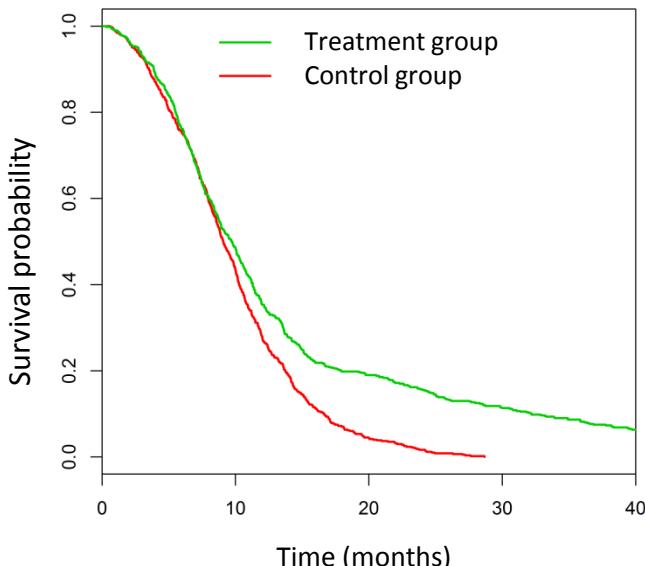


The net chance of a longer survival

Proportional
Hazards

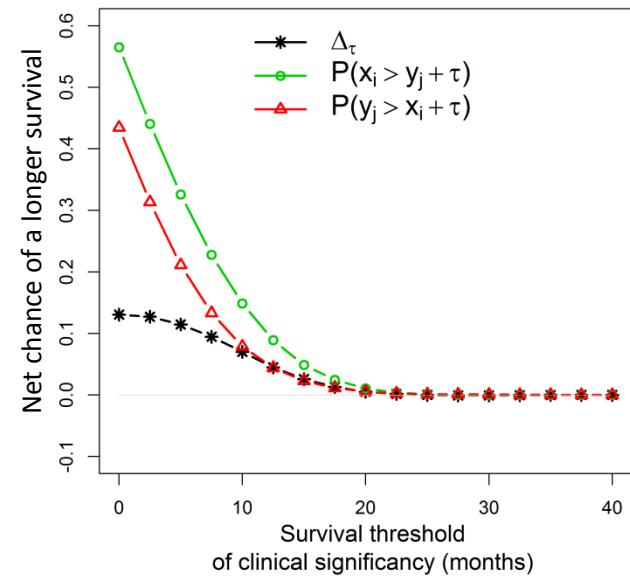
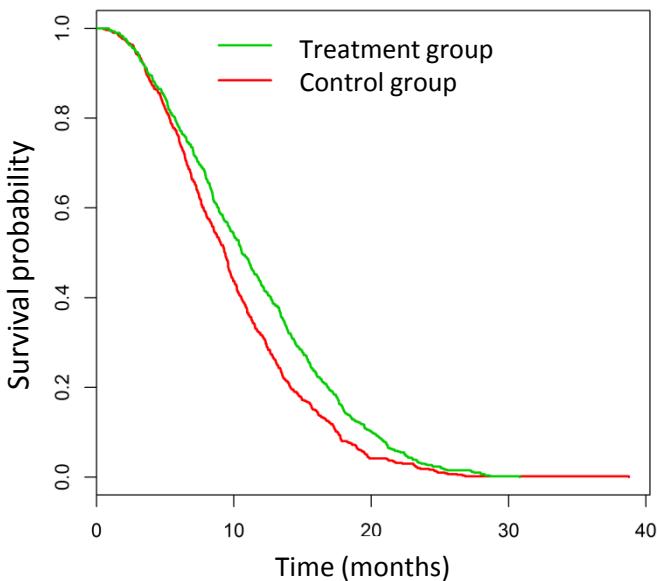


Delayed
treatment effect

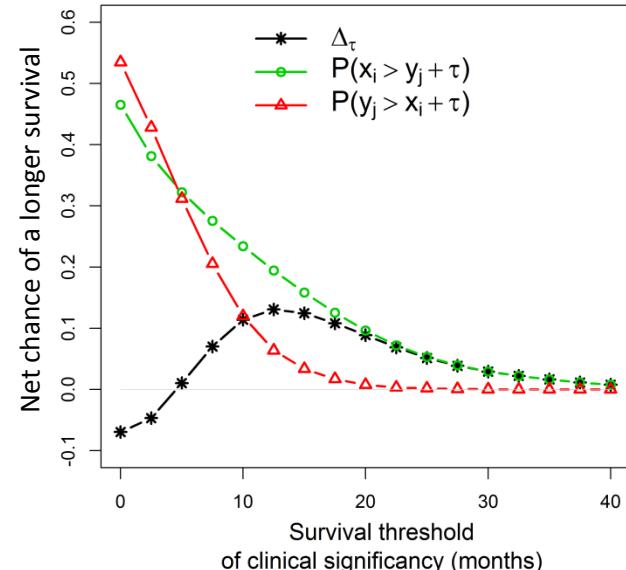
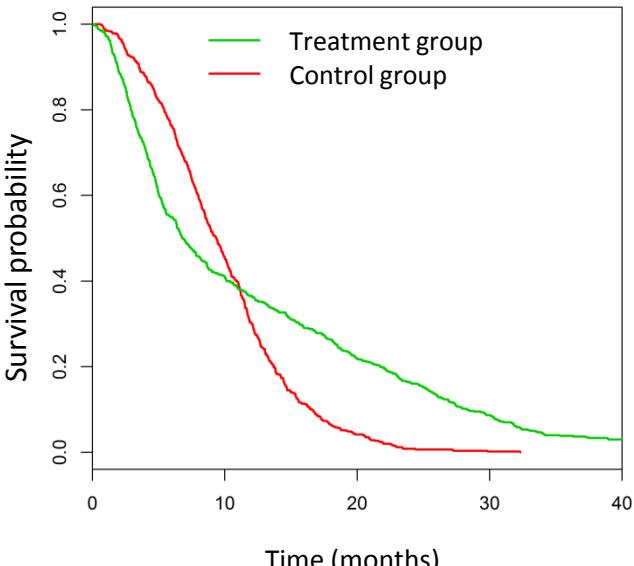


The net chance of a longer survival

Proportional
Hazards



Opposite
hazards

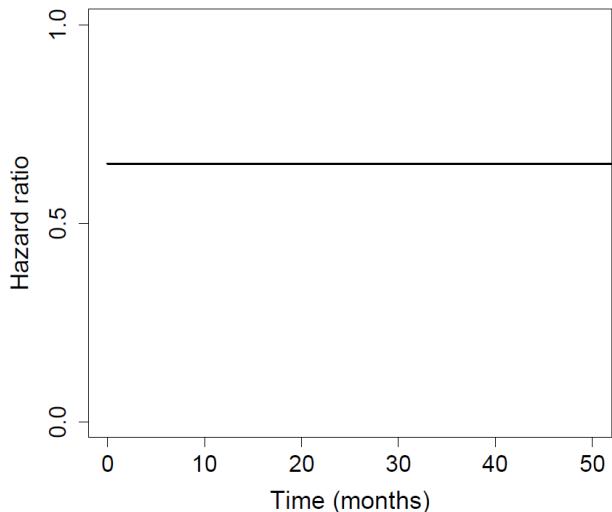


Simulation study - Design

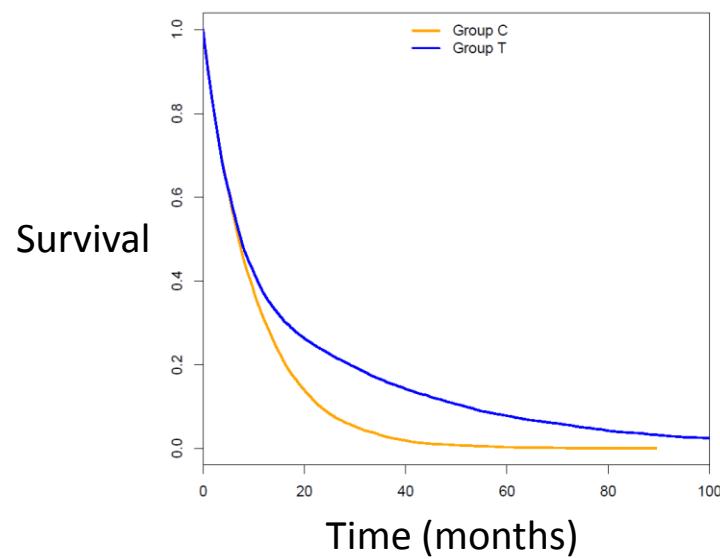
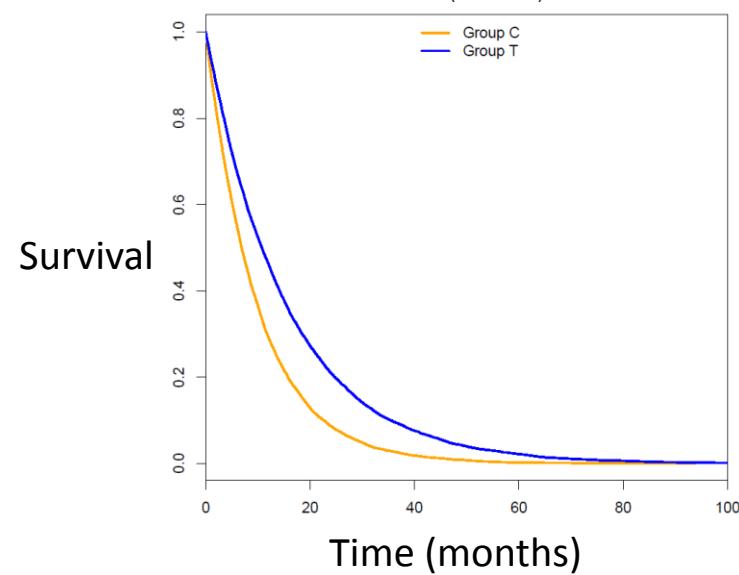
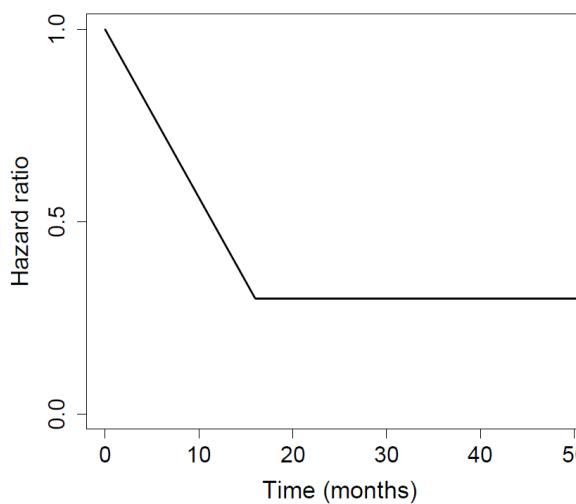
- **Objective:** To assess the power of tests based on generalized pairwise comparisons for delayed treatment effect
- Simulation of $M = 1000$ datasets of with $N = 200$ patients
 - One time-to-event outcome

Simulation study - Design

Scenario 1 : Proportional hazards



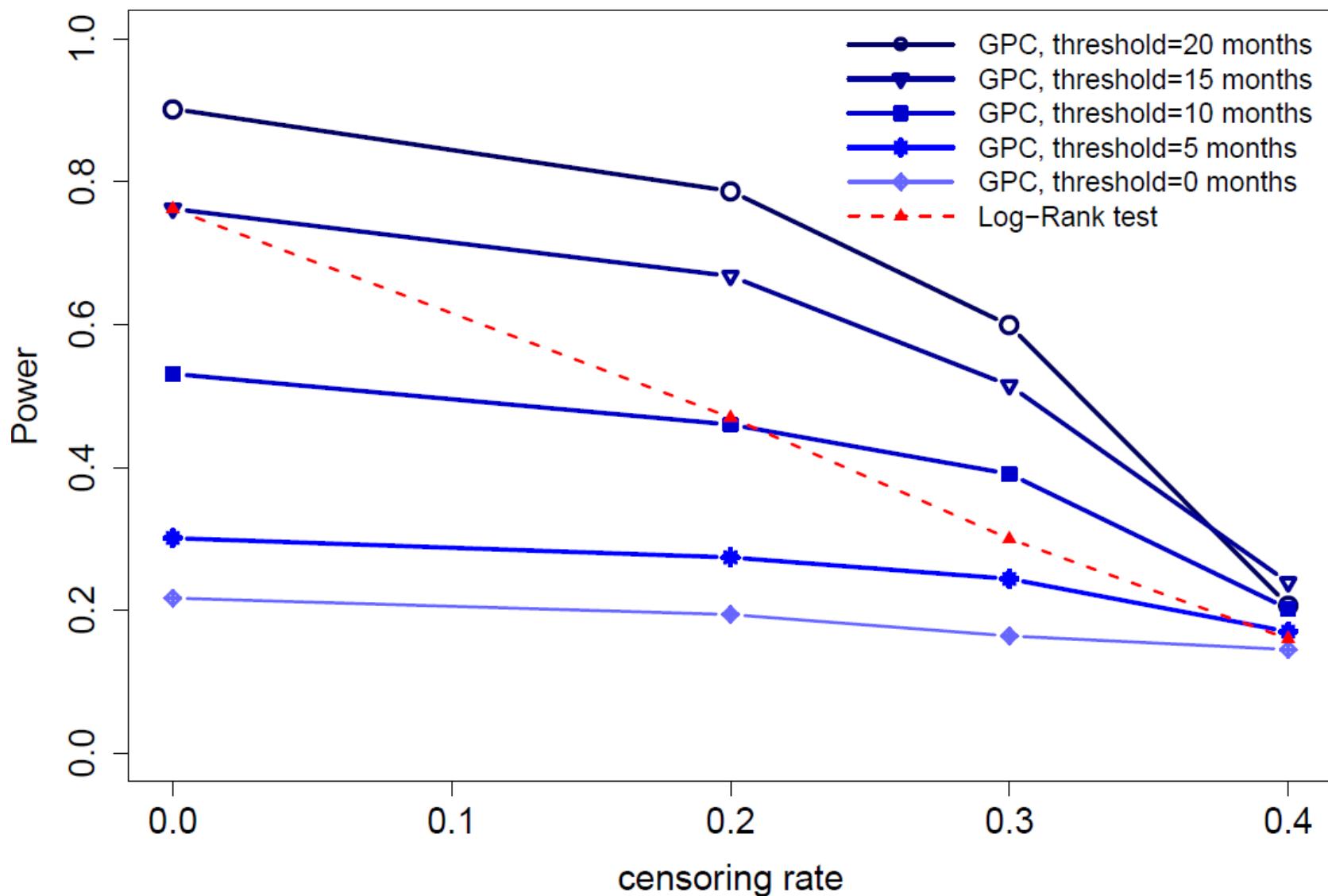
Scenario 2 : Late treatment effect



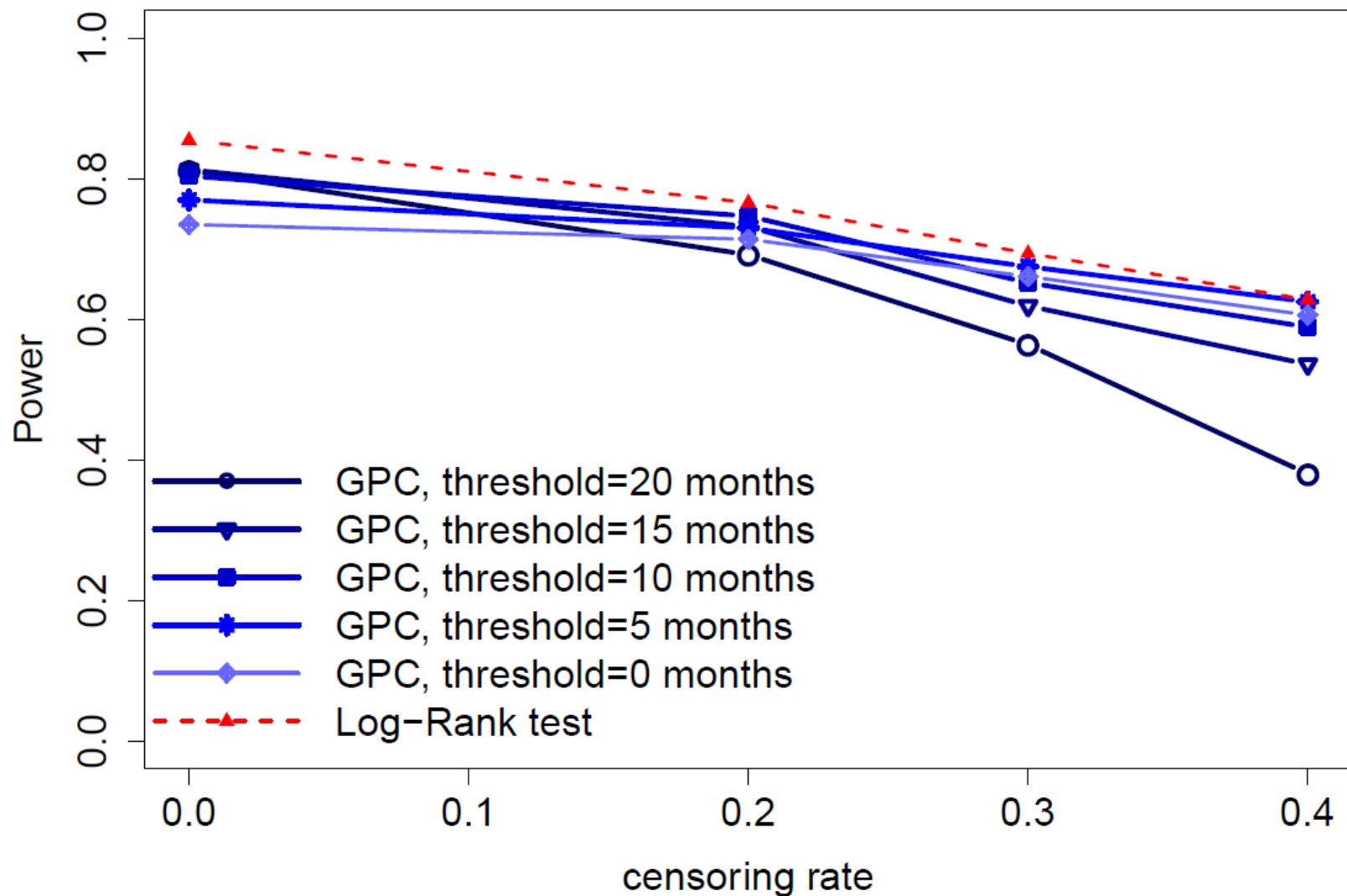
Simulation study - Design

- Administrative censoring proportion
 - Uniform distribution
 - Between 0% and 40%
- For each simulated dataset
 - Estimation of the net chance of a better outcome (extended procedure) with threshold τ [0 to 20 months]
 - Test of the null hypothesis (Permutation test, Log-Rank test)

Delayed treatment effect - POWER



Proportional Hazards - POWER



Conclusions

When a long-term survival benefit is expected
(anticancer immune therapy)

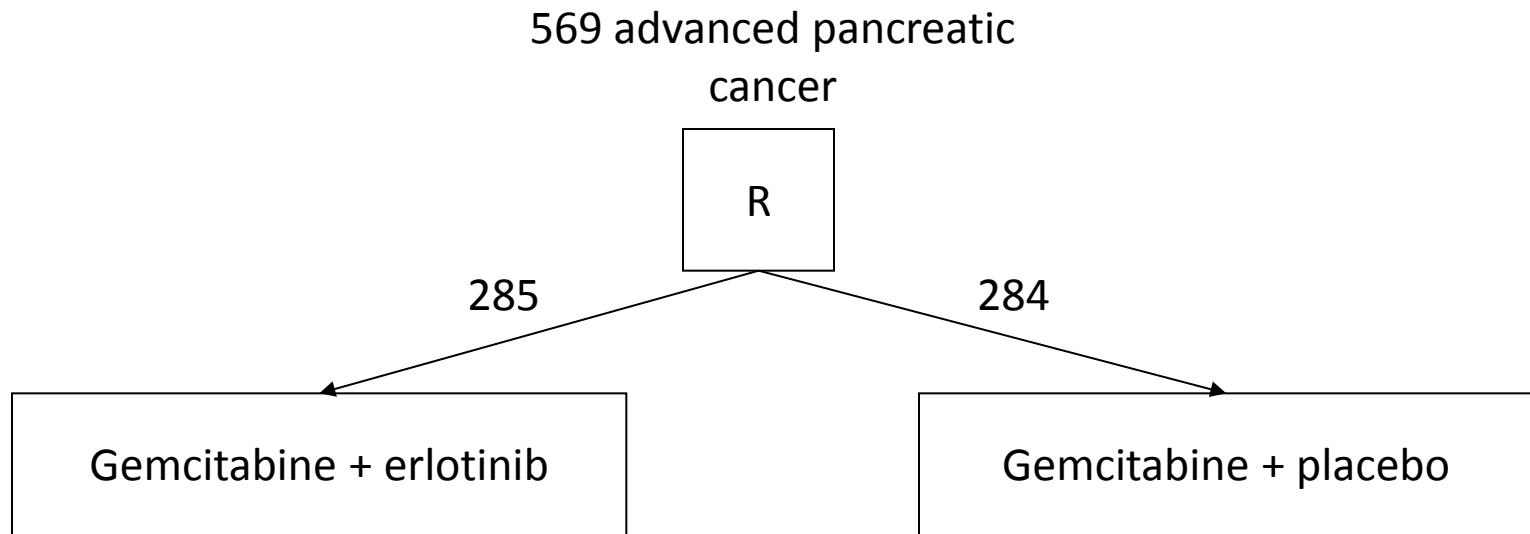
The net chance of a longer survival is:

- Arguably more relevant than traditional methods
- More powerful than traditional method

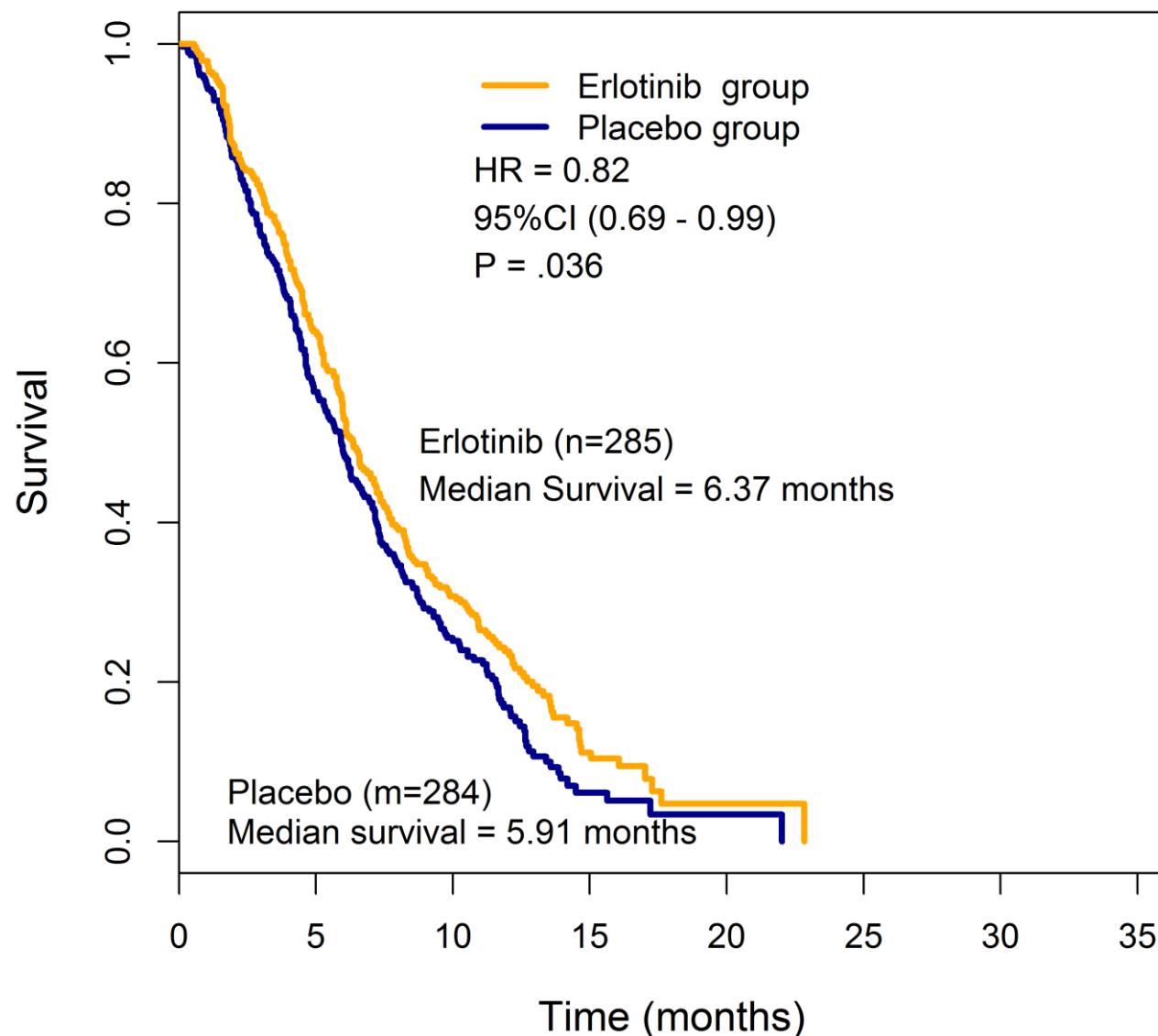
Outline

- The standard procedure of generalized pairwise comparisons
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- A patient-oriented measure of treatment benefit
- **Benefit-risk balance**
 - NCIC PA.3 trial => erlotinib in pancreatic cancer

The benefit-risk balance in the PA.3 trial



The benefit-risk balance in the PA.3 trial



The benefit-risk balance in the PA.3 trial

Worst grade related AE	Erlotinib group (n=282)	Placebo group (n=280)
Grade 1	48 (17%)	69 (24.6%)
Grade 2	118 (41.8%)	89 (31.8%)
Grade 3	72 (25.5%)	47 (16.8%)
Grade 4	11 (3.9%)	6 (2.1%)
Grade 5	4 (1.4%)	3 (1.1%)

The benefit-risk balance in the PA.3 trial

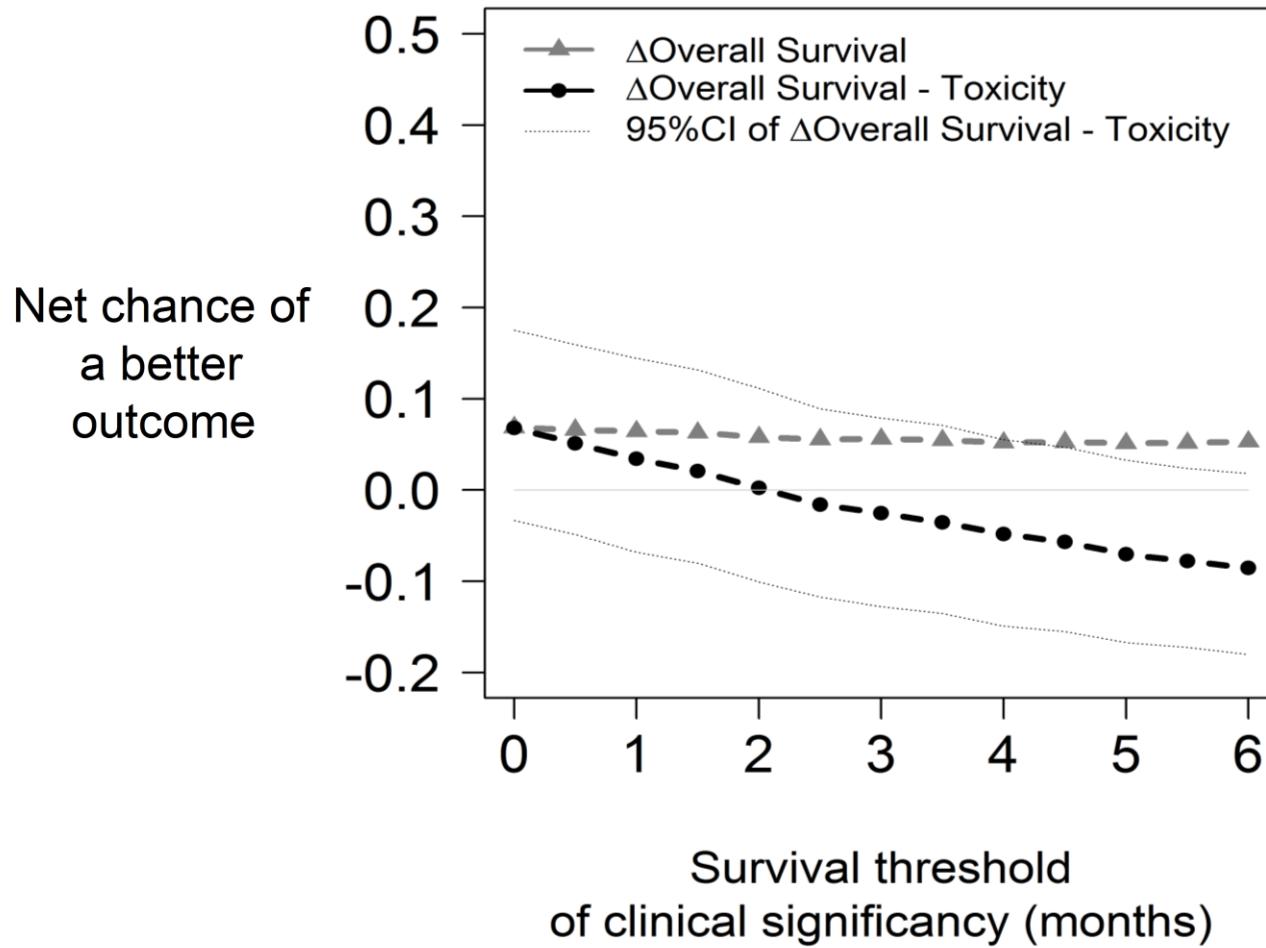
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Benefit-risk balance

Extended procedure

Priority	Erlotinib > Placebo	Placebo > Erlotinib	Δ [erlotinib]
1 : OS (Threshold = 2 months)	40.3 %	34.5 %	5.8 %
2 : Worst related AE grade	6.8 %	12.4 %	-5.6 %
Global	47.1 %	46.9 %	0.2 % (P=.96)

Benefit-risk balance



Software implementation

A package  corresponding to the standard procedure and to the extended procedure

- Available on CRAN (“BuyseTest”)
- Available on github
 (“<https://github.com/bozenne/BuyseTest>”)

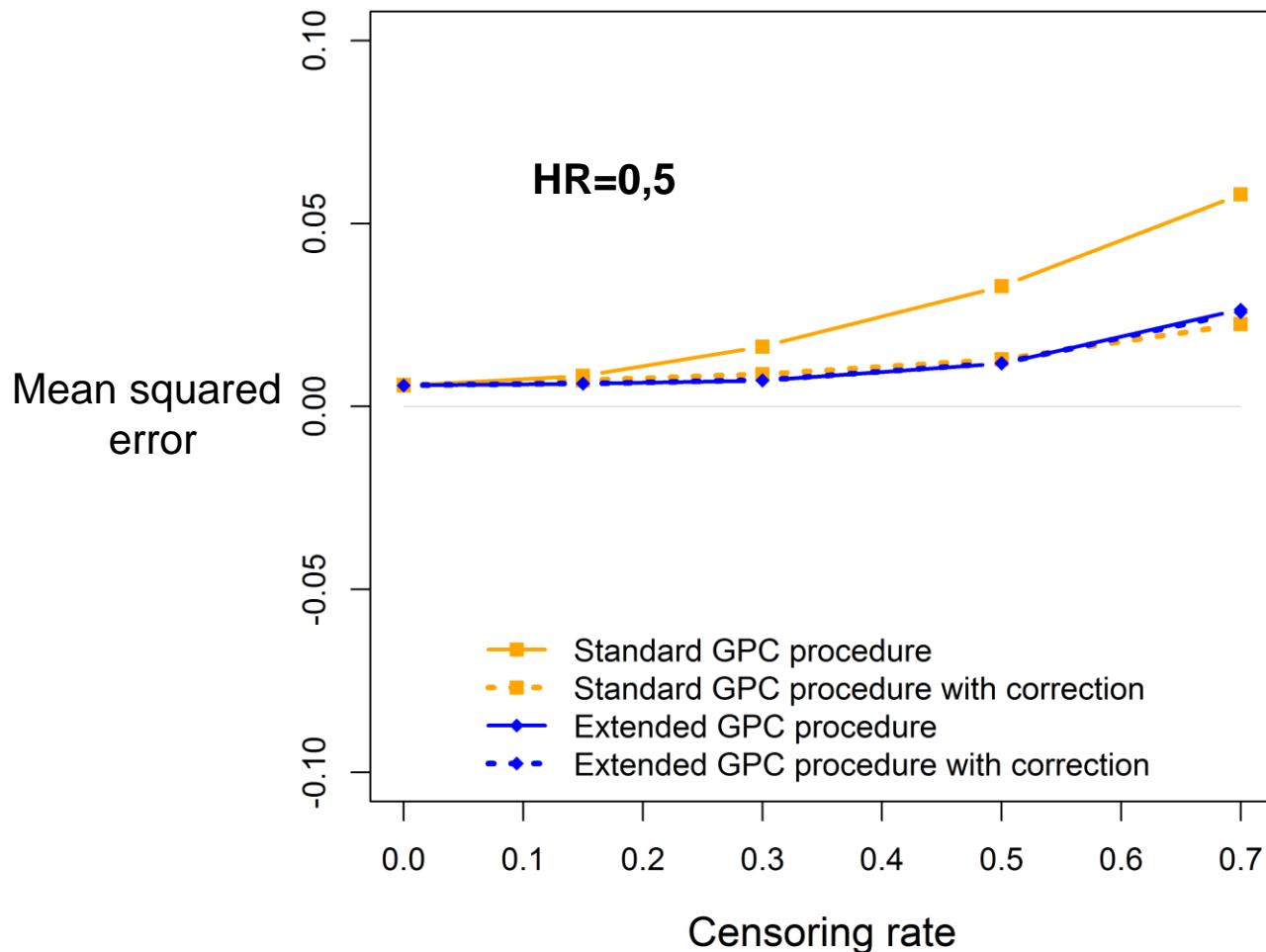
Conclusions

The net chance of a better outcome

- Is **flexible**
- Is **meaningful**
- Allows **multicriteria analysis**
- Can focus on **long-term survival differences**
- Is OK when hazards are **not proportionals**
- Is **available**

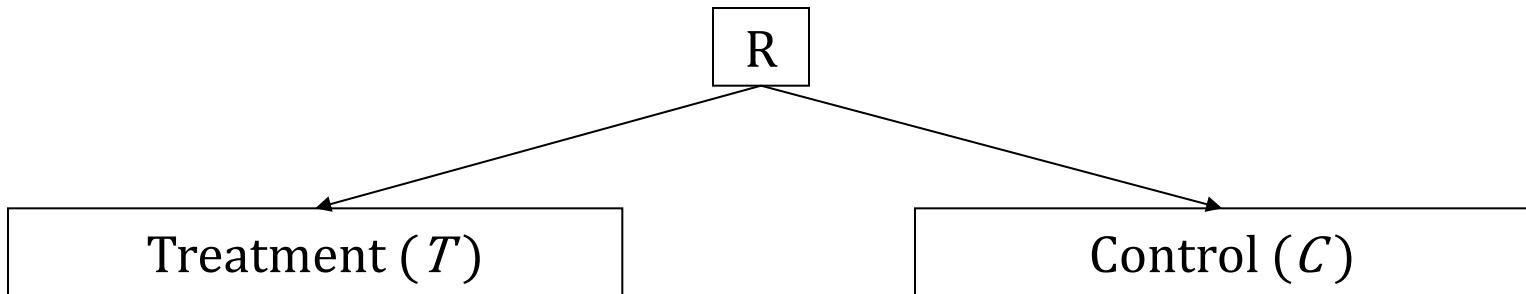
Thank you

Scénario 1 – Mean squared error



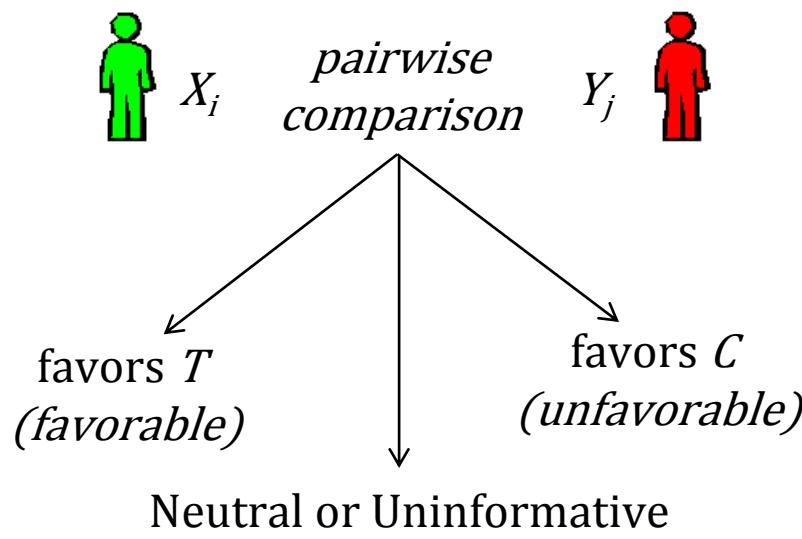
$$Mean\ squared\ error = \mathbb{E} \left((\hat{\Delta} - \Delta)^2 \right)$$

Methods – Pairwise comparisons



Let x_i be the outcome of
 i^{th} subject in T ($i = 1, \dots, n$)

Let y_j be the outcome of
 j^{th} subject in C ($j = 1, \dots, m$)



Methods – Definition of thresholds

Coutinuous outcome

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x_i or y_j missing	Uninformative

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Unfavorable	NA	Unfavorable
Uninformative	Favorable	Favorable
Uninformative	Unfavorable	Unfavorable
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Methods – Standard procedure for pairwise scoring

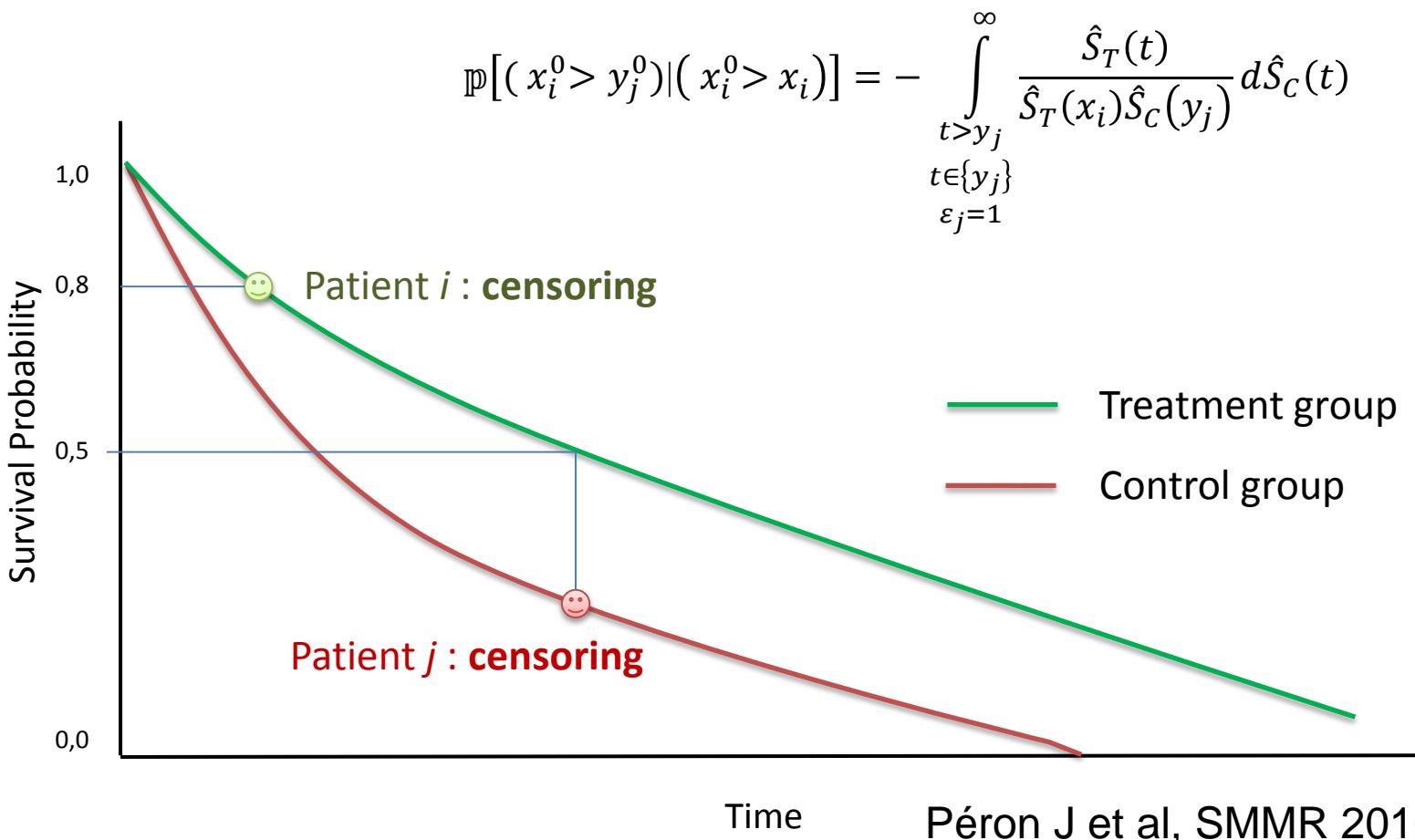
$$U_{ij} = \begin{cases} +1 & \text{when the pair } (X_i, Y_j) \text{ is favorable} \\ -1 & \text{when the pair } (X_i, Y_j) \text{ is unfavorable} \\ 0 & \text{otherwise} \end{cases}$$

$$\Delta = U = \frac{1}{m \cdot n} \sum_{i=1}^n \sum_{j=1}^m U_{ij}$$

Δ is named «chance of a better outcome»

The extended procedure taking into account 'non-informative' pairs

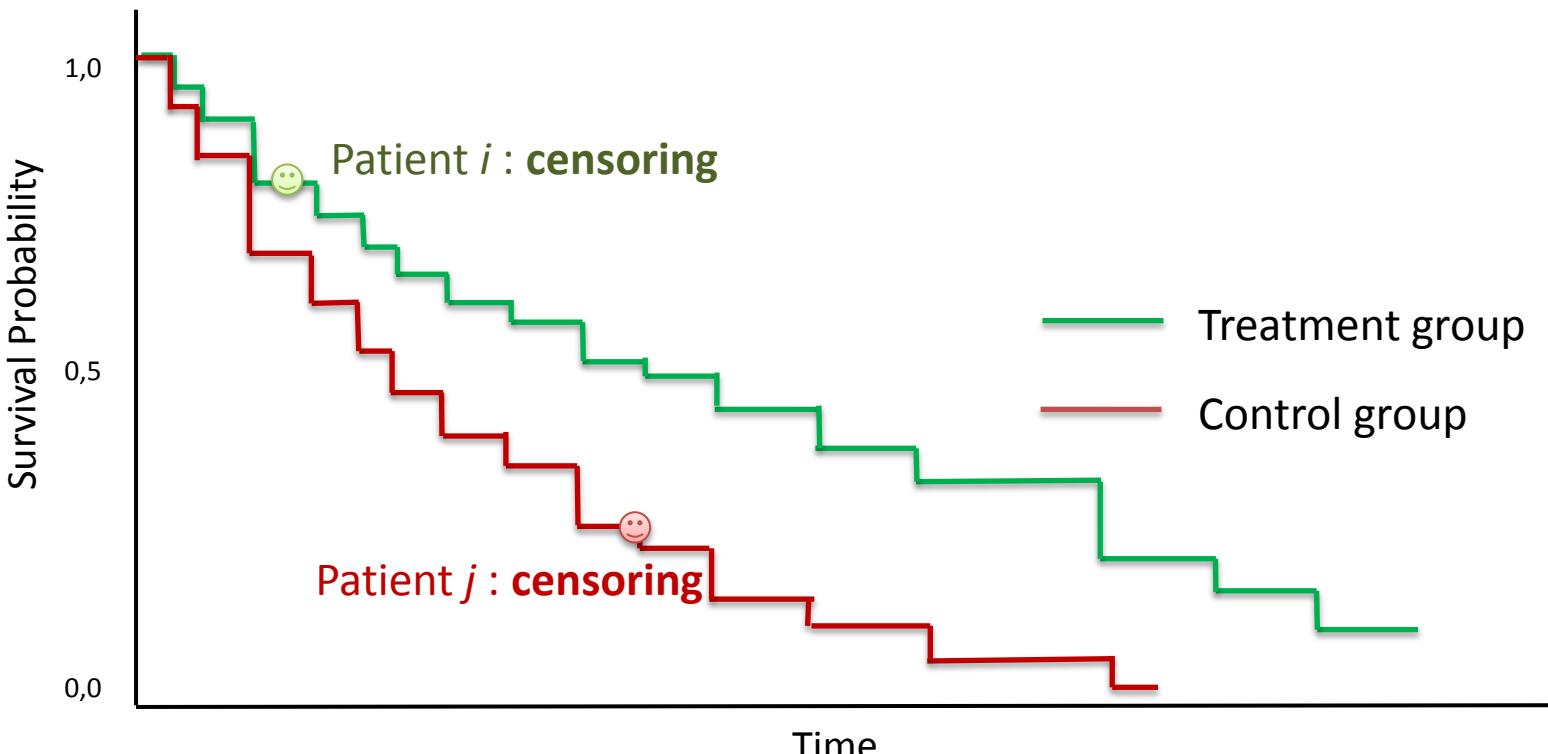
Based on the Kaplan-Meier estimate of the survival function



The extended procedure taking into account 'non-informative' pairs

When the estimation of the survival function is discontinue :

$$\mathbb{P}[(x_i^0 > y_j^0) | (x_i^0 > x_i), (y_j^0 > y_j)] = - \sum_{t > y_j}^{\infty} \frac{\hat{S}_{Ttt}(t)}{\hat{S}_{Ttt}(x_i)\hat{S}_{Ctrl}(y_j)} \cdot (\hat{S}_{Ctrl}(t^+) - \hat{S}_{Ctrl}(t^-))$$



Extension prenant en compte les temps jusqu à censure

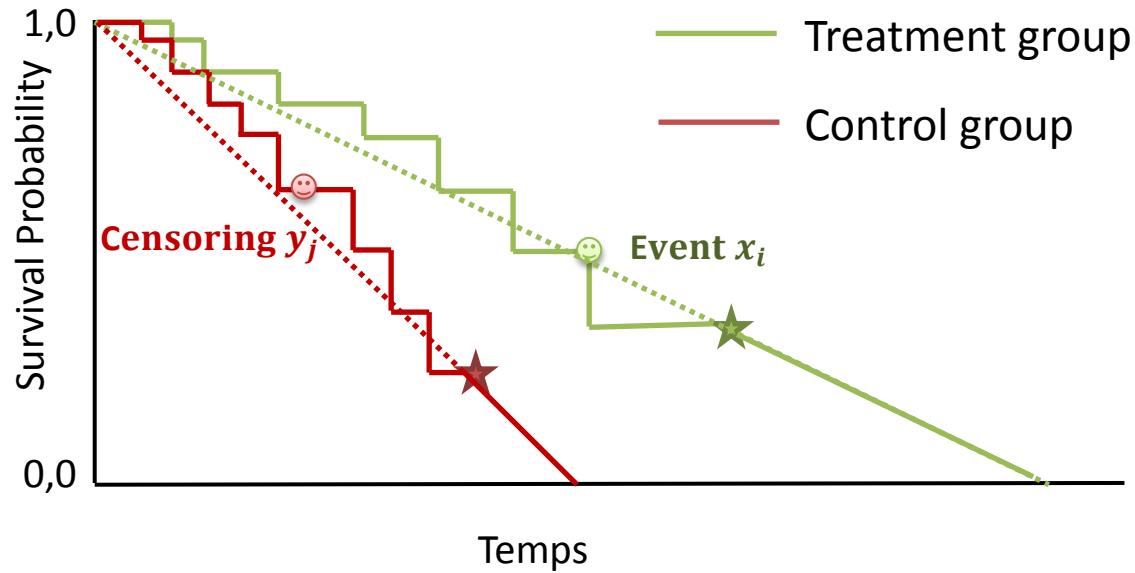
$(\delta_i, \varepsilon_j)$	$x_i - y_j > \tau$	$x_i - y_j < -\tau$	$ x_i - y_j < \tau$
$(1, 1)$	1	-1	0
$(0, 1)$	1	$\frac{\hat{S}_T(y_j + \tau) + \hat{S}_T(y_j - \tau)}{\hat{S}_T(x_i)} - 1$	$\frac{\hat{S}_T(y_j + \tau)}{\hat{S}_T(x_i)}$
$(1, 0)$	$1 - \frac{\hat{S}_C(x_i + \tau) + \hat{S}_C(x_i - \tau)}{\hat{S}_C(y_j)}$	-1	$-\frac{\hat{S}_C(x_i + \tau)}{\hat{S}_C(y_j)}$
$(0, 0)$	$1 - \frac{\hat{S}_C(x_i - \tau) + \hat{S}_C(x_i + \tau)}{\hat{S}_C(y_j)}$ $- \int_{\substack{t > y_j \\ t \in \{y_j\} \\ \varepsilon_j=1}}^{\infty} \frac{\hat{S}_T(t + \tau) + \hat{S}_T(t - \tau)}{\hat{S}_T(x_i) \hat{S}_C(y_j)} d\hat{S}_C(t)$ $- \int_{\substack{t > x_i - \tau \\ t \in \{y_j\} \\ \varepsilon_j=1}}^{\infty} \frac{\hat{S}_T(t + \tau)}{\hat{S}_T(x_i) \hat{S}_C(y_j)} d\hat{S}_C(t)$ $- \int_{\substack{t > x_i + \tau \\ t \in \{y_j\} \\ \varepsilon_j=1}}^{\infty} \frac{\hat{S}_T(t - \tau)}{\hat{S}_T(x_i) \hat{S}_C(y_j)} d\hat{S}_C(t)$	$- \int_{\substack{t > y_j \\ t \in \{y_j\} \\ \varepsilon_j=1}}^{\infty} \frac{\hat{S}_T(t + \tau) + \hat{S}_T(t - \tau)}{\hat{S}_T(x_i) \hat{S}_C(y_j)} d\hat{S}_C(t)$ -1	$- \int_{\substack{t > y_j \\ t \in \{y_j\} \\ \varepsilon_j=1}}^{\infty} \frac{\hat{S}_T(t + \tau)}{\hat{S}_T(x_i) \hat{S}_C(y_j)} d\hat{S}_C(t)$ $- \frac{\hat{S}_C(x_i + \tau)}{\hat{S}_C(y_j)}$

Valeurs du score attribué à chaque paire en fonction d'un seuil τ représentant la différence minimale cliniquement significative

Sensitivity analysis

Priority	Threshold	proportion of pairs (%)			Δ erlotinib
		Erlotinib > Placebo	Placebo > Erlotinib		
1 : OS	6 months	16.8	13.1		3.6
2 : PFS	6 months	3.0	1.8		1.2
3 : Worst related AE grade	3 grades	2.3	5.8		-3.5
4 : OS	3 months	11.2	10.8		0.4
5 : PFS	3 months	3.4	2.7		0.7
6 : Worst related AE grade	2 grades	2.3	6.0		-3.7
7 : OS	0 months	9.5	9.1		0.4
8 : PFS	0 months	0.5	0.6		-0.1
9 : Worst related AE grade	1 grade	0.2	0.5		-0.3
Overall		49.2	50.4		-1.2 (P=.82)

Hypothesis of the correction

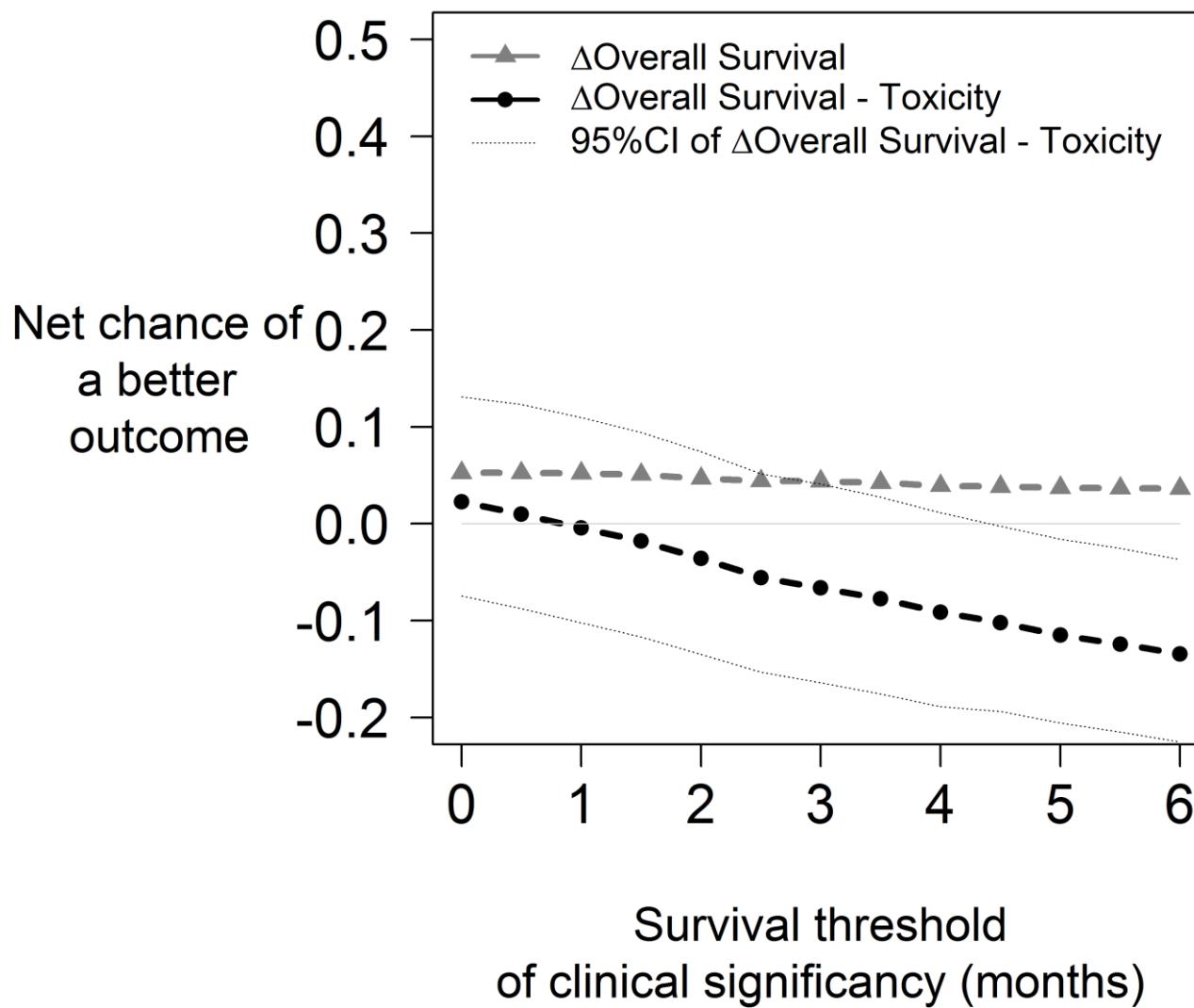


With the standard procedure

	proportion of pairs (%)		
	Erlotinib > Placebo	Placebo > Erlotinib	Δ erlotinib
1 : OS (Threshold = 2 months)	37.0	32.3	4.7
2 : Worst related AE grade	7.5	15.7	-8.3
Overall	44.5	48.1	-3.6 (P=.51)

Main analysis of the benefit-risk balance of the erlotinib and gemcitabine combination

Sensitivity analysis



Benefit-risk balance

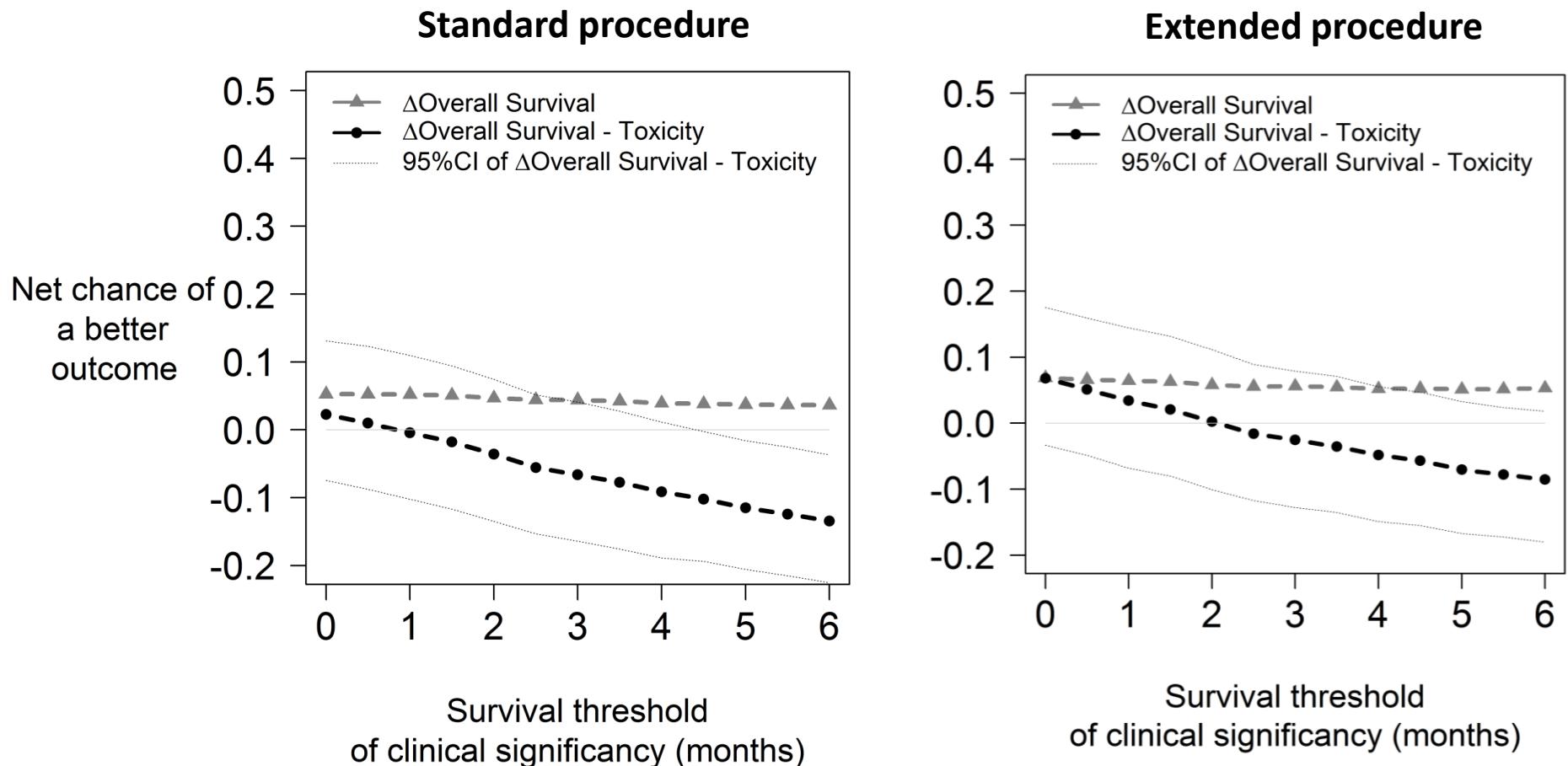
Standard procedure

Priority	Erlotinib > Placebo	Placebo > Erlotinib	Δ [erlotinib]
1 : OS (Threshold = 2 months)	37.0 %	32.3 %	4.7 %
2 : Worst related AE grade	7.5 %	15.7 %	-8.3 %
Global	44.5 %	48.1 %	-3.6% (P=.51)

Extended procedure

Priority	Erlotinib > Placebo	Placebo > Erlotinib	Δ [erlotinib]
1 : OS (Threshold = 2 months)	40.3 %	34.5 %	5.8 %
2 : Worst related AE grade	6.8 %	12.4 %	-5.6 %
Global	47.1 %	46.9 %	0.2 % (P=.96)

Benefit-risk balance



Benefit-risk balance

PRODIGE 4 trial

Priority	FOLFIRINOX > Gemcitabine	Gemcitabine > FOLFIRINOX	Δ [FOLFIRINOX]
1 : OS (Threshold = 2 months)	43.0%	21.7%	21.3%
2 : Worst related AE grade	8.2%	15.4%	-7.2%
Global	51.2%	37.1%	14.0% (P=0.029)

Benefit-risk balance

PRODIGE 4 trial

Priority	FOLFIRINOX > Gemcitabine	Gemcitabine > FOLFIRINOX	Δ [FOLFIRINOX]
1 : OS (Threshold = 2 months)	43.0%	21.7%	21.3%
2 : Worst related AE grade	8.2%	15.4%	-7.2%
Global	51.2%	37.1%	14.0% (P=0.029)

NCIC PA-3 trial

Priority	Erlotinib > Placebo	Placebo > Erlotinib	Δ [erlotinib]
1 : OS (Threshold = 2 months)	37.0 %	32.3 %	4.7 %
2 : Worst related AE grade	7.5 %	15.7 %	-8.3 %
Global	44.5 %	48.1 %	-3.6% (P=.51)

NCIC PA-3 trial

